Semi-supervised Document Classification Using Ontologies

by

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ABSTRACT

Many modern applications of automatic document classification require learning accurately with little training data. Addressing the need to reduce the manual labeling process, the semi-supervised classification technique has been proposed. This technique use labeled and unlabeled data for training and it has shown to be effective in many cases. However, the use of unlabeled data for training is not always beneficial and it is difficult to know a priori when it will be work for a particular document collection. On the other hand, the emergence of web technologies has originated the collaborative development of ontologies. Ontologies are formal, explicit, detailed structures of concepts.

In this thesis, we propose the use of Ontologies in order to improve automatic document classification, when we have little training data. We propose that making use of ontologies to assist the semi-supervised document classification can substantially improve the accuracy and efficiency of the semi-supervised technique.

Many learning algorithms have been studied for text. One of the most effective is Support Vector Machines, which is the basis of this work. Our algorithm enhances the performance of Transductive Support Vector Machines through the use of ontologies. We report experimental results applying our algorithm to three different real-world text classification datasets. Our experimental results show an increment of accuracy of 4% on average and up to 20% for some datasets, in comparison with the traditional semi-supervised model.
RESUMEN

Muchas aplicaciones modernas de la clasificación automática de documentos requieren obtener un clasificador eficiente utilizando pocos datos de entrenamiento. La técnica de clasificación semi-supervisada surgió con el fin de reducir el proceso de clasificación manual. Esta técnica utiliza en el entrenamiento tanto documentos etiquetados como no etiquetados y ha demostrado ser muy eficaz en muchos casos. Sin embargo, el uso de los datos no etiquetados no siempre es beneficioso y es difícil saber a priori cuándo es efectivo para una colección de documentos en particular. Por otro lado, la madurez de tecnologías web ha originado el desarrollo colaborativo de ontologías. Las ontologías son estructuras formales, explícitas y detalladas de conceptos.

En esta tesis se propone el uso de ontologías para mejorar la clasificación de documentos, cuando se tienen pocos datos de entrenamiento. Proponemos que el uso de ontologías en la clasificación semi-supervisada de documentos puede ayudar a mejorar considerablemente la precisión y la eficiencia.

El algoritmo de clasificación que utilizamos como base de nuestro trabajo es la versión semi-supervisada de las máquinas de vectores soporte, TSVM. Nuestro algoritmo mejora el rendimiento de los TSVM a través del uso de ontologías. Presentamos los resultados experimentales utilizando tres conjuntos de documentos. Los resultados experimentales muestran un incremento de la precisión del 4% en promedio y hasta un 20% para algunos conjuntos de datos, en comparación con el modelo TSVM.
To Karen Sofia
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1 INTRODUCTION

Automatic document classification has become an important subject due the proliferation of electronic text documents in the last years. This problem consists in learn to classify unseen documents into previously defined categories. The importance of make an automatic document classification is noticeable in many practical applications: Email filtering (Sahami et al., 1998), online news filtering (Chan et al., 2001), web log classification (Yu et al., 2005), social media analytics (Melville et al., 2009), etc.

Supervised learning methods construct a classifier with a training set of documents. This classifier could be seen as a function or decision rule that is used for classifying future documents into previously defined categories. Supervised text classification algorithms have been successfully used in a wide variety of practical domains. In experiments conducted by Namburú et al., using high accuracy classifiers with the most widely used document datasets, they report up to 96% of accuracy with a binary classification in the Reuters dataset. However, they needed 2000 manually labeled documents to achieve this good result (Namburú et al., 2005).

The problem with supervised learning methods is that they require a large number of labeled training examples to learn accurately. Manual labeling is a costly and time-consuming process, since it requires human effort. In some applications, this approach becomes impractical, since most users would not have time to spend in label thousands of documents. On the other hand, there exists many unlabeled documents readily available, and
it has been proved that in the document classification context, unlabeled documents are valuable and very helpful in the classification task (Nigam et al., 1998).

The use of unlabeled documents in order to assist the text classification task has been successfully used in numerous researches in the last years (Bennett et al., 1998), (Joachims, 1999), (Nigam, 2001), (Krithara et al., 2008). This process has received the name of semi-supervised learning. In experiments conducted by Nigam, on the 20 Newsgroups dataset, the semi-supervised algorithm performed well even with a very small number of labeled documents (Nigam et al., 1998). With only 20 labeled documents and 10,000 unlabeled documents, the accuracy of the semi-supervised algorithm was 5% superior than the supervised algorithm using the same amount of labeled documents.

Unfortunately, semi-supervised classification does not work well in all cases. In the experiments found in literature some methods perform better than others and for distinct datasets the performance differs (Namburú et al., 2005). There are some datasets that do not benefit from unlabeled data or even worst, sometimes, unlabeled data decrease performance. Nigam (Nigam et al., 1998) suggests two improvements to the probabilistic model in which he tries to contemplate the hierarchical characteristics of some datasets.

Another technique that is used to overcome the problem of manual labeling is Active Learning. Active Learning tries to minimize the annotation cost by labeling as few examples as possible and focusing in the most useful documents. Some researchers (Krithara, 2008), (Nigam et al., 1998), (Tong, 2001) have proposed the combination of both techniques semi-supervised learning and active learning, using active learning in the top of each iteration of
the semi-supervised learner. The disadvantage with this approach is that it still requires manual labeling of the most useful examples in every iteration of the learning algorithm. Thus, this approach is used only when the learning algorithm can interact with a human during the labeling effort.

Simultaneously, with the advances of web technologies, ontologies have increased on the World-Wide Web. Ontologies represent shared knowledge as a set of concepts within a domain, and the relationships between those concepts. The ontologies on the Web range from large taxonomies categorizing Web sites to categorizations of products for sale and their features. They can be used to reason about the entities within that domain, and may be used to describe the domain. In this thesis we propose the use of ontologies in order to assist the semi-supervised classification.

1.1 Motivation

In certain applications, the learner can generalize well using little training data. Even when it is proved that, for the case of document classification, unlabeled data could improve efficiency. However, the use of unlabeled data is not always beneficial, and in some cases it decreases performance.

Ontologies provide another source of information, which, with little cost, helps to attain good results when using unlabeled data. The kind of ontologies that we focus in this thesis give us the words we expect to find in documents of a particular class.
Using this information we could guide the direction of the use of unlabeled data, respecting the particular method rules. We just use the information provided by the ontologies when the learner needs to make a decision, and we give the most probable label when otherwise arbitrary decision is to be made.

The advantages of using ontologies are twofold:

- They are easy to get since they are either readily available or they could be built with little cost.
- Improve the time performance of the algorithm by speeding up convergence.

1.2 Problem Statement

Provide a learning approach that exploits the use of ontologies readily available, in order to assist the semi-supervised document classification task.

This method has to be efficient, effective and improve the benefits of traditional semi-supervised learning.

The method has to overcome the challenges of the semi-supervised learning from documents:

1. High dimensionality. Text classification deals with a large space of input documents and for each document, the corresponding vector has thousands of dimensions. Training classifiers in high dimensional spaces is a computational difficult problem. It is necessary to develop training algorithms that can handle the large number of features efficiently.
2. Limited training data. In most learning problems, the required number of training data has to be bigger than the dimension of the data, in order to learn accurately. In this case, we face the problem of having few labeled examples.

1.3 Contributions

In this thesis, we study and implement the use of ontologies in order to assist the semi-supervised document classification.

Our contributions are as follows:

1. Incorporate the use of ontologies to semi-supervised learning algorithms, in order to learn more accurate and more efficiently. Specifically, we modified the Transductive Support Vector Machine algorithm in order to make use of ontologies.

2. Provide an efficient implementation that works accurate and efficiently.

3. Present empirical evaluations that confirm our premise.

1.4 Summary of Following Chapters

Chapter 2 introduces the basic concepts and characteristics that are common in Text Mining Systems. We develop the necessary theoretical background in Chapter 3. Chapter 4 deals with the theoretical model for semi-supervised SVM using ontologies. In chapter 5 we present experiments and data analysis related to the semi-supervised SVM model using
ontologies. Conclusions are presented in Chapter 6. Chapter 7 presents the ethical considerations relative to this thesis.
2 BASICS IN TEXT MINING

Text mining, sometimes called Knowledge Discovery from Text (KDT), is the process of automatically analyzing text documents from different perspectives and extracting useful information from them. Text mining comes to be the analogue of data mining applied to text documents. Therefore, it derives much of its motivation, methodologies and direction from basic research on data mining.

Feldman and Sanger (Feldman et al., 2007) define Text Mining as a "knowledge-intensive process in which a user interacts with a document collection over time by using a suite of analysis tools". They emphasize that preprocessing is a major step in text mining compared to data mining since it involves significant processing steps for transforming a text into a structured format suitable for later analysis.

Hearst (Hearst, 1999) uses this metaphor for text mining: 'the use of large online text collections to discover new facts and trends about the world itself'. This point of view has a strong focus on undiscovered information within texts. Text mining includes exploratory data analysis that leads to the discovery of a priori unknown facts derived from texts, and hypothesis generation. The latter has successfully been applied in biology and medicine, such as investigations and medical hypothesis generation of causes for certain diseases by mining abstracts and texts of related biomedical literature (Fan et al., 2006).

Weiss et al. (Weiss et al., 2004) emphasize that text is different from classical input in data mining, and give a detailed explanation of necessary preprocessing steps due to the
nature of unstructured text. They also highlight the importance of texts in daily (private and business) communication and the importance of the use of predictive methods to analyze this kind of unstructured information.

In summary, text mining can be defined as:

- Automated Processing of Text.
- A knowledge-intensive process of text documents.
- Use of text collections to discover new facts.
- Analyzing unstructured information.
- Intelligent text processing.

2.1 Text Mining Technologies

As mentioned before, a central difference between text mining systems and data mining systems is that the former is designed to handle unstructured or semi-structured data from XML files and heterogeneous documents (such as email, full-text documents, and HTML files) (Fan et al., 2006).

![Figure 2-1 Generic architecture of text mining systems](image)

Figure 2-1 outlines a generic architecture of text mining systems. Starting with a collection of documents, a text-mining tool retrieves a particular document and preprocesses it. In order to run their knowledge discovery algorithms, text mining systems require
transforming raw, unstructured, original-format content into a carefully structured data format (Konchady, 2006). Once we have a structured data, we are ready to perform a text mining task in order to provide knowledge. Technologies in the text-mining process include information extraction, topic tracking, summarization, concept linkage, information visualization; question answering, document classification and clustering (Fan et al., 2006).

In this work, we are interested in the two latter technologies mentioned above: document classification and document clustering also known as supervised and unsupervised document classification respectively. We will explain them in detail in section 2.3. In the following, we will briefly describe the other technologies:

2.1.1 Information extraction

Information extraction looks for predefined sequences in the text (Fan et al., 2006). Information-extraction software should be able to identify people, places, companies, time, etc. and infer the relationships among all the identified objects to give the user meaningful information.

2.1.2 Topic tracking

A topic-tracking system predicts documents of interest to the user according user profiles, based on the documents a user examines, or letting users select particular categories of interest (Fan et al., 2006). There are many possible applications, for example it can be used for a company to keep track of news on itself and on its own products.
2.1.3 Concept linkage

Concept-linkage finds related documents by identifying their shared concepts, helping users find information they perhaps wouldn’t have found through traditional search methods (Fan et al., 2006).

2.1.4 Information Visualization

Information visualization consists in showing large textual sources in a visual hierarchy or map and providing browsing capabilities, in addition to simple searching (Fan et al., 2006).

2.2 Preprocessing

Data mining preprocessing focuses on tasks such as normalization, error detection and correction and dimension reduction. For text mining systems, preprocessing operations focus on the identification and extraction of representative features for natural language documents. These preprocessing operations are responsible for transforming unstructured data stored in document collections into a more explicitly structured intermediate format, which is a concern that is not relevant for most data mining systems (Feldman et al., 2007).

In the following we will describe the techniques for the transformation of unstructured text into structured formats.
2.2.1 Document standardization

Text documents exist in many formats, depending on how the documents were generated. If we will process all the documents, it is helpful to convert them to a standard format. Most of the text-processing community, has adopted XML (Extensible Markup Language) as its standard exchange format (Weiss et al., 2004). Many word processors allow documents to be saved in XML format, and stand-alone filters can be obtained to convert existing documents without having to process each one manually (Weiss et al., 2004).

The main advantage of standardizing the data is that the mining tools can be applied without having to consider the format of the document (Weiss et al., 2004).

2.2.2 Tokenization

The first step in handling text is to break the stream of characters into words or, more precisely, tokens (Weiss et al., 2004). A token is a more formal definition of a single unit of text. A single word may not be the smallest unit of text and a token may consist of one or more words (Feldman et al., 2007).

According to Konchady (Konchady, 2006), a token is a word, number, punctuation mark, or any other sequence of characters that should be treated as a single unit.

The accurate extraction of tokens is important for precise results in higher-level applications. Vector representations of documents used in document classification are made up of a sequence of tokens and weights. Documents can be correctly categorized only when the vector represents accurately the contents of documents (Konchady, 2006).
To get the best possible features, one should always customize the tokenizer for the available text, otherwise extra work may be required after the tokens are obtained. Note that the tokenization process is language-dependent. In this thesis, we focus on documents in English. For other languages, although the general principles will be the same, the details will differ (Weiss et al., 2004).

The algorithm for the single token extraction as proposed in (Konchady, 2006) is shown in Figure 2-2.

<table>
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<th><strong>Single_Tokens_Extraction</strong></th>
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<td><strong>Input</strong></td>
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<td><strong>Output</strong></td>
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1. Define the set of legal token characters (alphanumeric characters and optional characters) and initialize a token list.

2. Scan the text stream one character at a time; if the current character is not in the ASCII range of 32 to 122, assign a space to the character.
   a. If the current character is a token character:
      i. If the previous character was not a token character, add the previous token to the list and create a new token.
      ii. Concatenate the current character to the current token. Continue at step 2.
   b. Else, (if the current character is a space character):
      i. If the previous character was not a space, add the previous token to the list.
      ii. Create a new token with a space (consecutive space characters form one token). Continue at step 2.
   c. Default: All others characters turn into individual tokens.

3. Handle the last token.

*Figure 2-2 Algorithm for the single token extraction.*
The tokenization process described in Figure 2-2 (Konchady, 2006), consists of the following: A text stream is received as input. First, extract the single tokens. Then, assemble composite tokens using a set of rules and dictionary tables. Several passes are made over the list of tokens to find composite tokens such as abbreviations, numbers, internet tokens, and multi word tokens.

2.2.3 Stop Words Removal

An obvious reduction in dictionary size is to compile a list of 'stopwords' and remove them from the dictionary. These are words that almost never have any predictive capability, such as articles a and the and pronouns such as it and they. These common words can be discarded before the feature generation process, but it's more effective to generate the features first, apply all the other transformations, and at the very last stage reject the ones that correspond to 'stopwords' (Weiss et al., 2004).

2.2.4 Lemmatization or stemming

Stemming consists of converting each word to its stem. For instance, the words "taller" and "tallest" would both be converted to their stem "tall" (Larocca et al., 2000).

Whether or not this step is necessary is application-dependent. One effect of stemming is to reduce the number of distinct types in a document collection and to increase
the frequency of occurrence of some individual types. Stemming algorithms usually incorporate a great deal of linguistic knowledge, so that they are language-dependent.

Inflectional Stemming

Inflectional Stemming consists in regularize grammatical variants such as singular/plural and present/past. In English, with many irregular word forms and non-intuitive spelling, the process is not easy. There is no simple rule, for example, to bring together "seek" and "sought." Similarly, the stem for "rebelled" is "rebels," but the stem for "belled" is "bell" (Weiss et al., 2004).

According to (Weiss et al., 2004), an algorithm for inflectional stemming must be part rule-based and part dictionary-based. Any stemming algorithm for English that operates only on tokens, without more grammatical information such as part-of-speech, will make some mistakes because of ambiguity. Although the inflectional stemmer is not expected to be perfect, it will correctly identify quite a significant number of stems.

Stemming to a Root

Weiss (Weiss et al., 2004) defines stemming to a root as "the process of reaching a root form with no inflectional or derivational prefixes and suffixes". For example, "denormalization" is reduced to the stem "norm".

Extending the concept, we can also map synonyms to the same token. This adds a layer of complexity to the processing of text. Overall, stemming will achieve a large reduction in dictionary size.
2.2.5 Vectorization

Vector based representations has been widely used in text mining process for their simplicity. They are also referred to as a ‘bag of words’, emphasizing that document vectors are invariant with respect to term permutations, since the original word order in the document is clearly lost. However, many text retrieval and categorization tasks can be performed quite well in practice using the vector-space model.

The collective set of tokens or words is typically called a dictionary or vocabulary (V). They form the basis for creating the numeric vectors corresponding to the document collection.

More precisely, a text document \(d\) can be represented as a sequence of terms, \(d = (w_1, w_2, ..., w_{|d|})\), where \(|d|\) is the length of the document and \(w_t \in V\). A vector-space representation of \(d\) is then defined as a real vector \(x \in R^{|V|}\), where each component \(x_j\) is a statistic related to the occurrence of the \(j^{th}\) vocabulary entry in the document.

Note that typically the total number of terms in a set of documents is much larger than the number of distinct terms in any single document, \(|V| >> |d|\), so that vector-space representations tend to be very sparse. This property can be advantageously exploited for both memory storage and algorithm design.

The simplest vector-based representation is Boolean. In Boolean representation \(x_j \in \{0,1\}\) indicates the presence or the absence of term \(w_j\) in the document being represented.
Several refinements can be obtained by extending the Boolean vector model and introducing real-valued weights associated with terms in a document. Other vector-based representations are described in the next subsections.

**Term Frequency**

A more informative weighting scheme consists of counting the actual number of occurrences of each term in the document. This value may be multiplied by the constant $\frac{1}{|d|}$ to obtain a vector of term frequencies (TF) within the document.

Let $D = \{d_1, d_2, \ldots, d_n\}$ be a collection of documents. For each term $w_j \in V$, let $n_{ij}$ denote the number of occurrences of $w_j$ in document $d_i$. Then we define:

$$TF(w_j, d_i) = \frac{n_{ij}}{|d_i|}$$

The idea is that terms occurring most often in a document are more relevant than terms that do not. However, a frequent term may occur in almost every document. Such terms do not contribute to discriminate between classes. To assign lower weights to such term, sometimes the document frequency $DF(w_i)$ is used. This measure corresponds to the number of documents in which $w_i$ occurs at least once.

Finally, since documents can be of different length a normalization component adjusts the weights so that small and large documents can be compared on the same scale.
For example, the weight of term \( w_j \) in document \( d_i \) with normalized length according to \( L_2 \), is:

\[
x_{ji} = \frac{TF(w_j, d_i)}{\sqrt{\sum_j TF(w_j, d_i)^2}}
\]

**The TF-IDF weight**

An important family of weighting schemes combines term frequencies with inverse document frequency \( IDF \). As document frequency, inverse document frequency (IDF) is an ‘absolute' measure of term importance within the collection. \( IDF \) decreases as the number of documents in which the term occurs increases in a given collection. So terms that are globally rare receive a higher weight.

Let \( D = \{d_1, d_2, \ldots, d_n\} \) be a collection of documents and \( w_j \in V \), then we define:

\[
IDF_j = \log \frac{|D|}{DF(w_j)}
\]

The logarithmic function is employed as a damping factor.

Let \( \mathbf{x} = (x_{ij}) \) be the vector representation of the TF-IDF weight of term \( w_j \in V \) in document \( d_i \), it can be computed as:

\[
\mathbf{x} = TF(w_j, d_i) \cdot IDF_j
\]
Alternative versions of the basic TF-IDF exist. For example, the following weighting scheme uses TFIDF representation with normalized length according to $L_2$:

$$x = \frac{TF(w_j, d_i)IDF_j}{\sqrt{\sum_j (TF(w_j, d_i)IDF_j)^2}}$$

### 2.3 Document Classification

#### 2.3.1 Supervised classification

Automatic document classification consists in learning to classify unseen documents into previously defined categories. Given a collection of text documents and a set of categories, the task is to learn to predict the category for an unseen document.

We can describe supervised document classification as an automatic process with two phases:

**Learning Phase**

In the learning phase the system takes as its input a set of documents, which have been previously labeled, and learns a function $f$ from them. This assignment function is called a classifier. The labels that are assigned to the training documents belong to a predefined set of categories $C$.

Formally, the learner $\mathcal{L}$ is given a training set $S = \{(x_1, y_1), (x_2, y_2), ..., (x_n, y_n)\}$ of $n$ examples drawn according to an unknown probability distribution $\Pr(x, y)$. Each example consists of the document vector $x_i$ and the class label $y$. 
The process of learning consists in learning a function $f: D \times C \to \{-1,1\}$ where $D$ is the set of all possible documents and $C$ is the set of predefined categories. The value $f(x,y)$ is 1 if the document $x$ belongs to the category $y$ and -1 otherwise.

In other words, the system learns to predict the category of new documents.

**Prediction Phase**

In the prediction phase a new unlabeled document is presented to the system and it assigns a label according to the classifier it has learned.

![Figure 2-3 Supervised classification process](image)

The practical applications of supervised text classification are extensive. They vary from automatic email sorting (or specifically filtering spam emails) (Sahami et al., 1998), sentiment detection of a text or opinion mining (Pang et al., 2002), classification of news articles (Chan et al., 2001), classification of the e-commerce customer logs/notes (Yu et al., 2005), detecting a document's encoding (ASCII, Unicode, UTF-8, etc.), detecting the document language (English, Turkish, etc.) (Feinerer, 2008), etc.
Supervised text classification algorithms have been successfully used in a wide variety of practical domains. In experiments conducted by Namburú et al. (Namburú et al., 2005), using high accuracy classifiers with the most widely used document datasets, they report up to 96% of accuracy with a binary classification in the Reuters dataset. However, they needed 2000 manually labeled documents to achieve this good result.

The problem with the supervised learning methods is that they require a large number of labeled training examples to learn accurately. Manual labeling is a costly and time-consuming process, since it requires human effort. In some applications, this approach becomes impractical, since most users would not have time to spend in label thousands of documents (Nigam, 2001).

2.3.2 Supervised algorithms for document classification

There are many traditional learning methods which have shown good results on text classification problems in previous studies. Some of them, among others, are the following: Naïve Bayes classifier (Sahami et al., 1998), k-nearest neighbor classifier, Logistic Regression, Boosting (Weiss et al., 2004), Support Vector Machines (Joachims, 1998).

2.3.3 Unsupervised document classification

Unsupervised document classification, also known as document clustering, is a process through which documents are classified into meaningful groups called clusters, without any prior information. Any labels associated with objects are obtained exclusively from the data.
A clustering task may include a definition of proximity or similarity measure suitable to the domain. There are many possible similarity measures; however, the cosine similarity measure is the most common for text clustering:

Let \( \mathbf{x} \) and \( \mathbf{y} \) vector representations of two documents, and let \( n \) the dimension of the vectors.

\[
Sim(\mathbf{x}, \mathbf{y}) = \langle \bar{x}, \bar{y} \rangle = \sum_{k=1}^{n} \bar{x}_k \cdot \bar{y}_k
\]

where \( \bar{x} \) is the normalized vector \( \bar{x} = \frac{x}{\|x\|} \).

An unsupervised learning system takes as its input a collection of unlabeled documents. The system classifies documents according to a similarity measure and generates clusters of documents which are similar with certain probability. This description is depicted in Figure 2-4.

**Figure 2-4 Unsupervised classification process**

Document clustering is useful in a wide range of data analysis fields, including data mining, document retrieval, image segmentation, and pattern classification. Clustering methodology is especially appropriate in problems in which little prior information is
available and the system must make as few assumptions about the data as possible (Feldman et al., 2007).

An application of clustering is the analysis and navigation of big text collections such as Web pages. The basic assumption, called the cluster hypothesis, states that relevant documents tend to be more similar to each other than to non-relevant ones. If this assumption holds for a particular document collection, the clustering of documents based on the similarity of their content may help to improve the search effectiveness (Feldman et al., 2007).

2.3.4 Unsupervised algorithms document classification

Traditionally clustering techniques are divided in hierarchical and partitioning (Berkhin, 2002). Each of these can either be a hard clustering or a soft one. In a hard clustering, every object may belong to exactly one cluster. In soft clustering, the membership is fuzzy, objects may belong to several clusters with a fractional degree of membership in each (Feldman et al., 2007).

Hierarchical algorithms build clusters gradually. The basics of hierarchical clustering include the idea of conceptual clustering. Classic algorithms SLINK (Single LINKage), COBWEB, as well as newer algorithms CURE (Clustering Using Representatives) and CHAMELEON are in this category.

Partitioning algorithms learn clusters directly. In doing so, they either try to discover clusters by iteratively relocating points between subsets (Partitioning Relocation
Methods), or try to identify clusters as areas highly populated (Density-Based Partitioning). Partitioning Relocation Methods are further categorized into probabilistic clustering (EM (Expectation Maximization), framework algorithms (SNOB, AUTOCLASS, MCLUST), k-medoids methods like algorithms (Kaufman and Rousseeuw) PAM (Partitioning Around Medoids), CLARA (Clustering LARge Applications), CLARANS (clustering Large Application based upon Randomized Search) and its extensions, and k-means methods (different schemes initialization, optimization, harmonic means, extensions). Such methods concentrate on how well points fit into their clusters and tend to build clusters of proper convex shapes.

Many other clustering techniques are developed, that work well in particular scenarios. The most commonly used algorithms are the K-means, the EM-based mixture resolving (soft, flat, probabilistic), and the HAC (hierarchical, agglomerative).

The clustering of textual data has several unique features that distinguish it from other clustering problems. The most prominent feature of text documents as objects to be clustered is their very complex and rich internal structure. With big document collections, the dimension of the feature space may easily range into the tens and hundreds of thousands.

2.4 Related fields

There is a huge amount of contributions that underlines the cross-disciplinary research in text mining with connections to various related fields, like statistics, computer
science, or linguistics. In the following we will describe those which, we consider, are the most important:

2.4.1 Natural Language Processing

Text mining aims to extract or generate new information from textual information but does not necessarily need to understand the text itself. Instead, natural language processing tries to obtain a thorough impression on the language structure within texts. This allows a deeper analysis of sentence structures, grammar, morphology, and thus better retrieves the latent semantic structure inherent to texts (Feinerer, 2008). Some applications of natural language processing closely related to text mining are:

Automatic Summarization

Summarization reduces the length and detail of a document while retaining its main points and overall meaning (Fan et al., 2006). Text summarization helps users figure out whether a lengthy document meets their needs and is worth reading.

Question answering

Another application area of natural language processing is natural language queries, or question answering (QandA), which deals with how to find the best answer to a given question (Fan et al., 2006).
2.4.2 Information Retrieval

Information retrieval (IR) is concerned with searching for documents, for information within documents, and for metadata about documents, as well as that of searching relational databases and the World Wide Web.

Automated information retrieval systems are used to reduce overload of information. Many universities and public libraries use IR systems to provide access to books, journals and other documents. Web search engines are the most visible IR applications.
3 THEORETICAL BACKGROUND

In this chapter, we review the main theoretical fundamentals in which we base our thesis. We also provide a review of early work related to this thesis.

Section 1 introduces the optimization theory which is a fundamental block in the construction of Support Vector Machines. Section 2 introduces the naive Bayesian classification for text documents. Section 3 introduces the traditional Support Vector Machines applied to text documents. In Section 4 we give an overview of early work in semi-supervised document classification. Finally, section 5 introduces the concept of Ontology.

3.1 Optimization Theory

Optimization theory is the branch of mathematics that studies the extremal values of a function. It is concerned with determining the most profitable or least disadvantageous solution out of a set of alternatives and developing effective algorithms for finding them. Typically the set of alternatives is restricted by several constraints on the values of a number of variables and an objective function locates the optimum in the remaining set.

3.1.1 Mathematical Formulation

Optimization is the minimization or maximization of a function subject to constraints on its variables (Nocedal et al., 1999).

The general optimization problem can be stated as follows:
**Definition 3.1 (Primal Optimization Problem)**

Given functions $f, g_i, i=1,...,k$ and $h_i, i=1,...,m$, defined on a domain $\Omega \subseteq \mathbb{R}^n$,

$$\begin{align*}
\text{minimize}_{x \in \Omega} & \quad f(x) \\
\text{subject to} & \quad g_i(x) \leq 0, \quad i=1,...,k \\
& \quad h_i(x) = 0, \quad i=1,...,m
\end{align*}\tag{3-1}$$

where:

$x \in \Omega$ is the vector of variables, also called unknowns or parameters,

$f(x)$ is the objective function,

$g_i(x) \leq 0, i=1,2,...,k$ are the inequality constraints, and,

$h_i(x) = 0, i=1,2,...,m$ are the equality constraints.

The optimal value of the objective function is called the value of the optimization problem. The region of the domain where the objective function is defined and where all the constraints are satisfied is called the feasible region.

A solution of the optimization problem is a point $x^*$ in the feasible region such that there exists no other point $x$ in the feasible region for which $f(x) \leq f(x^*)$. Such a point is known as a global minimum. A point $x^*$ in the feasible region is called a local minimum of $f(x)$ if $\exists \varepsilon > 0$ such that $f(x) \geq f(x^*), \forall x \in \Omega$ such that $\|x - x^*\| < \varepsilon$.

The choice of minimization in definition 3.1 does not represent a restriction, since maximization problems can be converted to minimization ones by reversing the sign of the objective function and rewrite the constraints (Cristianini et al., 2002).
An inequality constraint \( g_l(x) \leq 0 \) is said to be active if the solution \( x^* \) satisfies \( g_l(x^*) = 0 \), otherwise is said to be inactive. Equality constraints are always active.

### 3.1.2 Convexity

The term convex can be applied both to sets and to functions (Nocedal et al., 1999).

**A set** \( S \in \mathbb{R}^n \) is a convex set if, for any two points \( x \in S \) and \( y \in S \), it follows that:

\[
ax + (1 - \alpha)y \in S \quad \text{for all } \alpha \in [0,1]
\]

**A function** \( f \) is a convex function if its domain \( D \) is a convex set, and for any two points \( x \in D \) and \( y \in D \), it follows that:

\[
f(ax + (1 - \alpha)y) \leq \alpha f(x) + (1 - \alpha)f(y) \quad \text{for all } \alpha \in [0,1]
\]

A function that is twice differentiable will be convex if its Hessian matrix is positive semi-definite (Cristianini et al., 2002). Convexity allows us to make strong claims about the convergence of optimization algorithms (Nocedal et al., 1999).

An affine function is one that can be expressed in the form \( f(x) = Ax + b \) for some matrix \( A \) and vector \( b \). Affine functions are convex since they have zero Hessian.

For the purpose of this work, we can restrict the study to the case where the constraints are all linear and the objective function is convex and quadratic.
3.1.3 Lagrange Duality

The purpose of Lagrangian theory is to characterize the solution of an optimization problem. It also leads to an alternative dual description, which often turns out to be easier to solve than the primal problem since handling inequality constraints directly is difficult (Cristianini et al., 2002).

For the simplest case, when there are no constraints, the stationarity of the objective function is sufficient to characterize the solution (Cristianini et al., 2002).

Theorem 3.1 (Fermat) A necessary condition for $x^*$ to be a minimum of $f(x), f \in C^1$, is

$$\frac{\partial f(x^*)}{\partial x} = 0$$

This condition, together with convexity of $f$, is also a sufficient condition.

In order to characterize the solution in constrained problems, it is necessary to define a function, known as the Lagrangian, that incorporates information about both the objective function and the constraints (Cristianini et al., 2002).

Definition 3.2 (Lagrangian Function)

Given an optimization problem with objective function $f(x)$, and equality constraints $h_i(x) = 0, i = 1, 2, \ldots, m$, the Lagrangian function is defined as

$$L(x, \beta) = f(x) + \sum_{i=1}^{m} \beta_i h_i(x)$$

where the coefficients $\beta_i$ are called the Lagrange multipliers.
If a point $x^*$ is a local minimum of $f(x), f \in C^1$, for a problem with only equality constraints, it is possible that $\frac{\partial f(x^*)}{\partial x} \neq 0$, but the directions in which we could move to reduce $f$ cause us to violate one or more of the constraints (Cristianini et al., 2002). In order to respect the equality constraint $h_i$, we must move perpendicular to $\frac{\partial h_i(x^*)}{\partial x}$, and so to respect all of the equality constraints we must move perpendicular to the subspace $V$ spanned by

$$\left\{ \frac{\partial h_i(x^*)}{\partial x}, i = 1, ..., m \right\}$$

if the $\frac{\partial h_i(x^*)}{\partial x}$ are linearly independent no legal move can change the value of the objective function, whenever $\frac{\partial f(x^*)}{\partial x}$ lies in the subspace $V$, or in other words when there exists $\beta_i$ such that

$$\frac{\partial f(x^*)}{\partial x} + \sum_{i=1}^{m} \beta_i h_i(x^*) = 0$$

**Theorem 3.2 (Lagrange)**

A necessary condition for a normal point $x^*$ to be a minimum of $f(x)$, subject to $h_i(x) = 0, i = 1, 2, ..., m$, with $f, h_i \in C^1$, is

$$\frac{\partial L(x^*, \beta^*)}{\partial x} = 0$$

$$\frac{\partial L(x^*, \beta^*)}{\partial \beta} = 0$$

for some values $\beta^*$. The above conditions are also sufficient provided that $L(x, \beta^*)$ is a convex function of $x$. 

30
The first of the 2 conditions gives a new system of equations, whereas the second condition returns the equality constraints. By jointly solving the two systems one obtain the solution.

**Definition 3.3 (Generalized Lagrangian function)**

Given an optimization problem defined on a domain $\Omega \subseteq \mathbb{R}^n$,

\[
\text{minimize}_{x \in \Omega} \quad f(x) \\
\text{subject to} \quad g_i(x) \leq 0, \quad i = 1, ..., k \\
\quad h_i(x) = 0, \quad i = 1, ..., m
\]

the Generalized Lagrangian function is defined as

\[
L(x, \alpha, \beta) = f(x) + \sum_{i=1}^{k} \alpha_i g_i(x) + \sum_{i=1}^{m} \beta_i h_i(x)
\]

where the coefficients $\alpha_i$ and $\beta_i$ are called the Lagrange multipliers.

**Definition 3.4 (Lagrangian dual problem)**

The Lagrangian dual problem of the primal problem of Definition 3.1 is the following problem:

\[
\text{maximize} \quad \theta(\alpha, \beta) \\
\text{subject to} \quad \alpha \geq 0,
\]

where $\theta(\alpha, \beta) = \inf_{x \in \Omega} L(x, \alpha, \beta)$. Lagrange multipliers are also called dual variables.
**Theorem 3.3 (Weak duality)**

Let \( x \in \Omega \) be a feasible solution of the primal problem of Definition 3.1 and \((\alpha, \beta)\) a feasible solution of the dual problem of Definition 3.4. Then \( f(x) \geq \theta(\alpha, \beta) \). (Cristianini et al., 2002)

**Corollary 3.1**

The value of the dual is upper bounded by the value of the primal.

**Corollary 3.2**

If \( f(x^*) = \theta(\alpha^*, \beta^*) \), where \( \alpha^* \geq 0 \) and \( g_i(x^*) \leq 0, h_i(x^*) = 0 \), then \( x^* \) and \( (\alpha^*, \beta^*) \) solve the primal and dual problem respectively. In this case \( \alpha_i^* g_i(x^*) = 0 \), for \( i = 1, \ldots, k \).

The solutions of the primal and dual having the same value is not in general guaranteed. The difference between the values of the primal and the dual problems is known as the **duality gap**.

**Theorem 3.4 (Strong duality)**

Given an optimization problem with *convex* domain \( \Omega \subseteq \mathbb{R}^n \),

\[
\begin{align*}
\text{minimize}_{x \in \Omega} & \quad f(x) \\
\text{subject to} & \quad g_i(x) \leq 0, \quad i = 1, \ldots, k \\
& \quad h_i(x) = 0, \quad i = 1, \ldots, m
\end{align*}
\]

where \( g_i \) and \( h_i \) are affine functions, that is \( h_i(x) = Ax - b \) for some matrix \( A \) and some vector \( b \), then the duality gap is zero.
Theorem 3.5 (Kuhn-Tucker)

Given an optimization problem with convex domain $\Omega \subseteq \mathbb{R}^n$, 

\[
\text{minimize}_{x \in \Omega} \quad f(x)
\]

subject to 
\[
g_i(x) \leq 0, \quad i = 1, \ldots, k
\]
\[
h_i(x) = 0, \quad i = 1, \ldots, m
\]

with $f \in C^1$ convex and $g_i$ and $h_i$ affine, necessary and sufficient conditions for a point $x^*$ to be an optimum are the existence of $\alpha^*, \beta^*$ such that:

(Karush-Kuhn-Tucker (KKT) conditions)

\[
\frac{\partial L(x^*, \alpha^*, \beta^*)}{\partial x} = 0
\]

\[
\frac{\partial L(x^*, \alpha^*, \beta^*)}{\partial \beta} = 0
\]

\[
\alpha_i^* g_i(x^*) = 0, \quad i = 1, \ldots, k
\]

\[
g_i(x^*) \leq 0, \quad i = 1, \ldots, k
\]

\[
\alpha_i^* \geq 0, \quad i = 1, \ldots, k
\]

The third relation is known as the Karush-Kuhn-Tucker (KKT) complementary condition. It implies that for inactive constraints, $\alpha_i^* = 0$. Perturbing inactive constraints has no effect on the solution of the optimization problem.

We can transform the primal problem into its corresponding dual by setting to zero the derivatives of the Lagrangian with respect to the primal variables, and substituting the resulting relations back into the Lagrangian. In this way we remove the dependence of the
primal variables. The resulting function contains only dual variables and must be maximized under simpler constraints (Cristianini et al., 2002).

3.2 Naive Bayesian Text Classification

3.2.1 The probabilistic model

In order to model the data, Naïve Bayes classifiers assume that documents are generated by a mixture of multinomial distributions model, where each mixture component corresponds to a class.

Bayes’ rule says that to achieve the highest classification accuracy, a document should be assigned to the class \( y \) for which \( P(y|d) \) is highest.

Suppose that \( C \) is the number of classes, the vocabulary is of size \( |V| \), and each document \( d_i \) has \( |d_i| \) words in it.

The likelihood of seeing document \( d_i \) is a sum of total probability over all mixture components. That is,

\[
P(d_i|\theta) = \sum_{j=1}^{C} P(c_j|\theta)P(d_i|c_j;\theta) \tag{3-3}
\]

Using the above along with standard Naive Bayes assumption: that the words of a document are conditionally independent among them, given the class label, we can expand the second term of equation 3-3, and express the probability of a document given a mixture
component in terms of its constituent features: the document length and the words in the document.

\[ P(d_i|c_j; \theta) \approx P(|d_i|) \prod_{w_t \in V} P(w_t|c_j; \theta)^{N_{it}} \]  

Where \( N_{it} \) refers to the number of times word \( w_i \) occurs in document \( d_i \).

The full generative model, given by combining equations 3-3 and 3-4, assigns probability \( P(d_i|\Theta) \) to generate document \( d_i \) as follows:

\[ P(d_i|\theta) \approx P(|d_i|) \sum_{j=1}^{c} P(c_j|\theta) \prod_{w_t \in V} P(w_t|c_j; \theta)^{N_{it}} \]  

3.2.2 Dirichlet distribution

Let \( p = (p_1, ..., p_k) \) a random vector such that \( \sum_{i=1}^{k} p_i = 1 \), \( 0 < p_i < 1 \), \( i = 1, ..., k \).

The Dirichlet distribution with parameters \( \alpha_1, \alpha_2, ..., \alpha_k \) is given by:

\[ P(p|\alpha_1, ..., \alpha_k) = \frac{\Gamma(\sum_{k=1}^{K} \alpha_k)}{\prod_{k=1}^{K} \Gamma(\alpha_k)} \prod_{k=1}^{K} p_k^{\alpha_k-1} \]  

Where an \( \alpha \) with large components correspond to strong prior knowledge about the distribution and \( \alpha \) with small components correspond to ignorance.

3.2.3 Multinomial Naive Bayes using Dirichlet Prior

Using maximum a posteriori (MAP) to estimate the parameters of a multinomial distribution with Dirichlet prior, yields:
Given estimates of these parameters, it is possible to calculate the probability that a particular mixture component generated a given document to perform classification. By applying Bayes rule it follows that:

\[
\tilde{\theta}_{w_t|c_j} = \frac{P(w_t|c_j; \theta) \prod_{w_t \in V} P(w_t|c_j; \tilde{\theta})^{N_{it}}}{\sum_{k=1}^{C} P(c_k|\tilde{\theta}) \prod_{w_t \in V} P(w_t|c_j; \tilde{\theta})^{N_{it}}}
\]

Then, to classify a test document into a single class, the class with the highest posterior probability is selected. See more details in (Mitchel, 2005).

### 3.3 Support Vector machines (SVM)

The learning method of Support Vector Machines (SVM) was introduced by Vladimir Vapnik et al (Boser et al., 1992). Supervised support vector machine technique has been successfully used in text domains (Joachims, 1998).

Support Vector Machines is a system for efficiently training linear learning machines in kernel-induced feature spaces. Linear learning machines are learning machines that form linear combinations of the input variables (Cristianini et al., 2002).
3.3.1 Notation

In order to describe SVM, first let us introduce some notation for the learning problem. Let $X \subseteq \mathbb{R}^n$ denote the input space and $Y$ denote the output domain. For binary classification $Y = \{-1, 1\}$, for $m$-class classification $Y = \{1, 2, \ldots, m\}$. 

3.3.2 Binary Linear Classification

Let $f : X \subseteq \mathbb{R}^n \rightarrow \mathbb{R}$ be a real-valued function, the input $x = (x_1, \ldots, x_1)'$ is assigned to the positive class, if $f(x) \geq 0$, and otherwise to the negative class. In the case that $f(x)$ is a linear function of $x \in X$, it can be written as the equation of an hyperplane:

$$f(x) = \langle w, x \rangle + b = \sum_{i=1}^{n} w_i x_i + b$$

where $w$ is the unit normal vector of the hyperplane and $b$ is the distance from the origin (see Figure 3-1).

![Figure 3-1 A hyperplane defined by the normal vector $w$ at a distance $b$ from the origin for a two dimensional training set.](image)
Then, the decision rule is given by $\text{sgn}(f(x))$. The parameters that control the learning function and must be learned from the data are $(w, b) \in \mathbb{R}^n \times \mathbb{R}$. The hyperplane defined by the function above is called the decision boundary.

The quantities $w$ and $b$ are usually called the weight vector and bias, respectively. Sometimes $b$ is replaced by $\theta$ and is called threshold (Cristianini et al., 2002).

If there exists a hyperplane that correctly classifies the training data, we say that the data are linearly separable. If no such hyperplane exists the data are said to be nonseparable. Intuitively, we can see that if a point is far from the separating hyperplane, then we may be significantly more confident in the prediction for the value of $y$ at this point. And, for a given training set, it would be good if we manage to find a decision boundary that allows us to make all correct and confident predictions on the training examples (meaning far from the decision boundary). We will formalize this later using the concepts of margins.

### 3.3.3 Geometric and Functional Margins

#### Geometric Margin

The geometric margin of some input example $x \in X$ is the distance from this point to the decision boundary. In Figure 3-2, let the point at A represent the input $x_i$ of some training example with label $y_i = 1$. Its distance to the decision boundary $\gamma_i$ is given by the line segment $\overline{AB}$. The direction of the vector $\overline{AB}$ is given by the unit-length vector $\frac{w}{||w||}$. Therefore $B$ is given by $x_i - \gamma_i \frac{w}{||w||}$.
Since B lies on the decision boundary then it satisfies the equation:

$$\langle w, x \rangle + b = w'.x + b = 0$$

Hence,

$$w'.(x_i - \gamma_i \frac{w}{\|w\|}) + b = 0$$

$$w'.x_i - \gamma_i \frac{w'.w}{\|w\|} + b = 0$$

$$w'.x_i - \gamma_i \frac{\|w\|^2}{\|w\|} + b = 0$$

$$\gamma_i \|w\| = w'.x_i + b$$

$$\gamma_i = \frac{w'}{\|w\|} \cdot x_i + \frac{b}{\|w\|}$$

Making the analogous process for the case of a negative example we get:
In general, we define the geometric margin of an hyperplane \((w, b)\) with respect to a training example \((x_i, y_i)\) to be

\[
y_i = -\frac{(w' \cdot x_i + b)}{||w||}
\]

It is worth noting that the geometric margin is invariant to rescaling of the parameters to \((\lambda w, \lambda b)\), \(\lambda \in \mathbb{R}^+\). This fact will be useful later.

Finally, giving a training set \(S = \{(x_i, y_i); i = 1, 2, ..., m\}\), we define the geometric margin of an hyperplane \((w, b)\) with respect to \(S\) to be the smallest of the geometric margins on the individual training examples.

\[
y = \min_i y_i
\]

**Functional Margin**

We define the functional margin of an hyperplane \((w, b)\) with respect to a training example \((x_i, y_i)\) to be the quantity:

\[
y_i = y_i (w' \cdot x_i + b)
\]

If \(y_i = 1\), then for the functional margin to be large, and in consequence, for our prediction to be confident and correct, we need \(w' \cdot x_i + b\) to be a large positive number. In the other hand, if \(y_i = -1\), then for the functional margin to be large, we need \(w' \cdot x_i + b\) to be a large negative number. Furthermore, \(\hat{y}_i > 0\) implies correct classification of \((x_i, y_i)\). Thus, a large functional margin represents a confident and a correct prediction.
Since the geometric margin equals the functional margin when $\|\mathbf{w}\| = 1$, thus geometrical and functional margin are related by $\gamma = \frac{\varphi}{\|\mathbf{w}\|}$.

Note that in the definition of linear classifiers there is an inherent degree of freedom, due to the fact that the function associated with the hyperplane $(\mathbf{w}, b)$ does not change if we rescale the hyperplane to $(\lambda \mathbf{w}, \lambda b), \lambda \in \mathbb{R}^+$. There will, however, be a change in the (functional) margin as measured by the function output as opposed to the geometric margin (Cristianini et al., 2002).

The functional margin distribution of a hyperplane $(\mathbf{w}, b)$ with respect to a training set $S = \{(\mathbf{x}_i, y_i); i = 1, 2, ..., m\}$, is the distribution of the margins of the examples in $S$. We refer to the minimum of the functional margin distribution as the functional margin of a hyperplane $(\mathbf{w}, b)$ with respect to a training set $S$.

### 3.3.4 The Maximal Margin Classifier

The maximal margin classifier is the simplest model of Support Vector Machine. It tries to find a decision boundary that maximizes the geometric margin, since this would reflect very confident predictions on the training set. For this model, we assume that the training data are linearly separable.

Since we are trying to maximize the geometrical margin $= \frac{\varphi}{\|\mathbf{w}\|}$, we can pose the following optimization problem:
maximize_{\gamma,w,b} \frac{\hat{y}_i}{\|w\|}

subject to \ y_i(w^\top x_i + b) \geq \hat{y}_i, \ i=1,2,...,m

With this formulation we have the problem that the objective function $\frac{\hat{y}_i}{\|w\|}$ is not a convex one, and hence, it is difficult to solve. However, we can make use of the fact that we can multiply $w$ and $b$ by an arbitrary scale constant without changing neither the decision function nor the geometric margin. Since multiplying $w$ and $b$ by some constant results in the functional margin being multiplied by that same constant, we can equally well optimize the geometric margin by fixing the functional margin to be equal to 1 and minimizing the norm of the weight vector $w$. Indeed, maximizing $\frac{\hat{y}_i}{\|w\|} = \frac{1}{\|w\|}$ is the same as minimizing $\|w\|^2 = \langle w,w \rangle$. Now, we have the following proposition:

**Proposition 3.1**

Given a linearly separable training set $S = \{(x_i, y_i); i = 1,2,...,m\}$, the hyperplane $(w,b)$ that solves the optimization problem

$$\minimize_{w,b} \frac{1}{2} \langle w,w \rangle$$

s.t. $y_i((w^\top x_i) + b) \geq 1, \ i=1,...,m$

releases the maximal margin hyperplane with geometric margin $\gamma = \frac{1}{\|w\|}$.

This is an optimization problem that can be efficiently solved, given that it has a convex quadratic objective function with linear constraints. Its solution give us the **maximal margin classifier**.
**Dual Formulation**

Using the Lagrange theory outlined in section 3.1.3, we transform the optimization problem of Proposition 3.1 into its corresponding dual problem.

The primal Lagrangian is

\[
L(w, \alpha, b) = \frac{1}{2} \langle w, w \rangle - \sum_{i=1}^{m} \alpha_i [y_i (\langle w, x_i \rangle + b) - 1]
\]

where \( \alpha_i \geq 0 \) are the Lagrangian multipliers.

Differentiating with respect to \( w \) and \( b \)

\[
\frac{\partial L(w, \alpha, b)}{\partial w} = w - \sum_{i=1}^{m} \alpha_i y_i x_i = 0
\]

\[
\frac{\partial L(w, \alpha, b)}{\partial b} = \sum_{i=1}^{m} \alpha_i y_i = 0
\]

From which we get:

\[
w = \sum_{i=1}^{m} \alpha_i y_i x_i
\]

\[
0 = \sum_{i=1}^{m} \alpha_i y_i
\]

Substituting back into the primal to obtain:
Proposition 3.2

Given a linearly separable training set \( S = \{(x_i, y_i); i = 1, 2, ..., m\} \), and suppose the parameters \( \alpha^* \) solve the following quadratic optimization problem:

\[
W(\alpha) = \sum_{i=1}^{m} \alpha_i - \frac{1}{2} \sum_{i,j=1}^{m} \alpha_i \alpha_j y_i y_j \langle x_i, x_j \rangle \\
\text{s.t. } \sum_{i=1}^{m} \alpha_i y_i = 0 \\
\alpha_i \geq 0, i = 1, ..., m
\]

then the weight vector \( w^* = \sum_{i=1}^{m} \alpha_i^* y_i x_i \) is a normal vector for the maximal margin hyperplane with geometric margin \( \gamma = \frac{1}{\|w\|} \).

Since the value of \( b^* \) does not appear in the dual problem, it must be found making use of the primal constraints:

\[
b^* = -\frac{\max_{y_i = -1}((w^* \cdot x_i)) + \min_{y_i = 1}((w^* \cdot x_i))}{2}
\]

Theorem 3.5 (Kuhn-Tucker) applies to this optimization problem. The KKT complementary conditions for this problem state:
This means that for inputs $\mathbf{x}_i$ for which the functional margin is one and that therefore lie closest to the hyperplane the corresponding $\alpha_i^*$ are non-zero. In consequence, in the expression for the weight vector only this points are involved (Cristianini et al., 2002). For this reason they are called \textit{support vectors}, see Figure 3-3.

\[ \alpha_i^* [y_i(\langle \mathbf{w}^*, \mathbf{x}_i \rangle + b^*) - 1] = 0, \quad i = 1, \ldots, m \]

\[ f(\mathbf{x}, \alpha^*, b^*) = \sum_{i=1}^{m} \alpha_i^* y_i (\mathbf{x}_i, \mathbf{x}) + b^* \]

\textbf{Figure 3-3 Optimal margin linear classifier. The examples closest to the hyperplane are called support vectors.}

The optimal hyperplane can be expressed in the dual representation in terms of this support vectors. Let $SV$ be the set of indices of the support vectors:
Hence, given \( \alpha_i^*, b^* \), the decision function depends only on the inner product between \( x \) and the support vectors.

Another important result of the KKT complementary conditions, as described in (Cristianini et al., 2002) is that for \( j \in SV \)

\[
y_j f(x_j, \alpha^*, b^*) = y_j \left( \sum_{i \in SV} \alpha_i^* y_i \langle x_i, x_j \rangle + b^* \right) = 1
\]

and consequently:

\[
\langle w^*, w^* \rangle = \sum_{i,j=1}^{m} \alpha_i^* \alpha_j^* y_i y_j \langle x_i, x_j \rangle
\]

\[
= \sum_{j \in SV} \alpha_j^* y_j \sum_{i \in SV} \alpha_i^* y_i \langle x_i, x_j \rangle
\]

\[
= \sum_{j \in SV} \alpha_j^* (1 - y_j b^*)
\]

\[
= \sum_{j \in SV} \alpha_j^*
\]

And therefore, we have the following proposition (Cristianini et al., 2002).

**Proposition 3.3**

Given a linearly separable training set \( S = \{(x_i, y_i); i = 1, 2, ..., m\} \), and suppose the parameters \( \alpha^* \) and \( b^* \) solve the quadratic optimization problem of Proposition 3.2. Then the
weight vector $w^* = \sum_{i=1}^{m} \alpha_i^* y_i x_i$ is a normal vector for the maximal margin hyperplane with geometric margin

$$\gamma = \frac{1}{||w||} = \left( \sum_{j \in S_V} \alpha_j^* \right)^{-\frac{1}{2}}.$$ 

This property is exploited in the next section with the use of Kernels.

### 3.3.5 Kernels

In real situations, data usually is not linear separable. To handle this problem, input data is transformed from its original space into another space so that a linear decision boundary can separate the data. The original data space is called **input space** and the transformed space is called **feature space**.

The idea is to map the data in the input space $X$ to a feature space $F$ via a nonlinear mapping $\varphi$, 

$$\varphi: X \rightarrow F$$

$$x \rightarrow \varphi(x)$$

The same linear SVM solution is then applied to $F$.

An important fact is that explicit transformation could be avoided, noting that in the dual representation both the construction of the optimal hyperplane and the evaluation of the corresponding classification function only require the evaluation of dot products. This is done through the use of **kernel functions**.
Definition 3.5 (Kernel)

A Kernel is a function \( K \), such that for all \( x, z \in X \)

\[
K(x, z) = \langle \varphi(x), \varphi(z) \rangle
\]

Kernel functions are sometimes more precisely referred to as Mercer kernels, because they must satisfy Mercer's condition, which guarantees that a kernel function must be continuous, symmetric, and have a positive definite Gram matrix (Cristianini et al., 2002). Such a means that there exists a mapping to a reproducing kernel Hilbert space (a Hilbert space is a vector space closed under dot products) such that the dot product there gives the same value as the function \( K \).

Proposition 3.4

Given a training set \( S = \{(x_i, y_i); i = 1, 2, ..., m\} \), that is linearly separable in the feature space implicitly defined by the kernel \( K(x, z) \) and suppose the parameters \( \alpha^* \) and \( b^* \) solve the following quadratic optimization problem:

\[
\begin{align*}
\text{maximize}_{w,b} & \quad W(\alpha) = \sum_{i=1}^{m} \alpha_i - \frac{1}{2} \sum_{i,j=1}^{m} \alpha_i \alpha_j y_i y_j K(x_i, x_j) \\
\text{s.t.} & \quad \sum_{i=1}^{m} \alpha_i y_i = 0 \\
& \quad \alpha_i \geq 0, i = 1, ..., m
\end{align*}
\]  

(3-13)

Then the decision rule given by \( sgn(f(x)) \), where \( f(x) = \sum_{i=1}^{m} \alpha_i^* y_i K(x_i, x) + b^* \) is equivalent to the maximal margin hyperplane in the feature space implicitly defined by the kernel \( K(x, z) \) and that hyperplane has geometric margin.
There are many different kernel functions; some of them are listed below.

Linear

$$K(\mathbf{x}, \mathbf{z}) = (\mathbf{x}, \mathbf{z})$$

Polynomial (homogeneous)

$$K(\mathbf{x}, \mathbf{z}) = (\mathbf{x}, \mathbf{z})^d, d \in \mathbb{N}$$

Polynomial (inhomogeneous)

$$K(\mathbf{x}, \mathbf{z}) = (\mathbf{x}, \mathbf{z} + 1)^d, d \in \mathbb{N}$$

Gaussian Radial Basis Function:

$$K(\mathbf{x}, \mathbf{z}) = \exp(-\gamma\|\mathbf{x} - \mathbf{z}\|^2), \gamma > 0$$

In this thesis a linear kernel was used. More explanation on kernel functions can be found in the book (Cristianini et al., 2002).

### 3.3.6 Soft Margin Optimization

If the data is noisy, there will in general be no linear separation in the feature space (Cristianini et al., 2002). To handle the problem of non-linearly separable data, slack variables are introduced to allow the margin constraints to be violated.
2-norm Soft Margin

This approach consists in solving the generalized optimal plane (GOP) problem (Bennett et al., 1998) given by:

\[
\min_{w,b,C} C \sum_{i=1}^{l} n_i + \frac{1}{2} \| w \|^2
\]

\[\text{s.t. } y_i (w \cdot x_i - b) + n_i \geq 1 \]

\[n_i \geq 1, i = 1, \ldots l\]

Where \( C > 0 \) is a penalty parameter. For each point, is added a slack term \( n_i \) such that if the point is misclassified, \( n_i \geq 1 \).

1-norm Soft Margin

A Robust Linear Programming approach is presented in (Bennett, 1992). It considers the use of the 1-norm instead of the 2-norm, \( \| w \|_1 = \sum_{j=1}^{n} | w_j | \). The problem becomes the following optimization problem:

\[
\min_{w,b,s,C} C \sum_{i=1}^{l} n_i + \sum_{j=1}^{n} s_j
\]

\[\text{s.t. } y_i (w \cdot x_i - b) + n_i \geq 1 \]

\[n_i \geq 0, i = 1, \ldots l\]

\[-s_j \leq w_j \leq s_j, j = 1, \ldots n\]
3.3.7 Multiclass discrimination

We can also solve the problem of binary classification by defining a weight vector $w_i$ and bias $b_i$ for each class (Cristianini et al., 2002). When a new instance $x$ has to be classified, both functions are evaluated, and the point $x$ is assigned to class $1$ if $\langle w_1, x \rangle + b_1 \geq \langle w_{-1}, x \rangle + b_{-1}$, otherwise $x$ is assigned to class $-1$. This approach is equivalent to discrimination using the single hyperplane $(w_1 - w_{-1}, b_1 - b_{-1})$ (Cristianini et al., 2002).

This approach could be used for multiclass discrimination with output domain $Y = \{1, 2, ..., m\}$. For each class, define a weight vector $w_i$ and bias $b_i$, and the decision function is given by

$$c(x) = \arg \max_i (\langle w_i, x \rangle + b_i)$$

This is equivalent to associating a hyperplane to each class, and to assigning a new point $x$ to the class whose hyperplane is furthest from it (Cristianini et al., 2002).

3.4 Semi-supervised Document Classification

The general idea of semi-supervised learning is to use a small number of labeled examples and a large number of unlabeled examples to achieve high-accuracy classification. The motivation for the use of unlabeled documents for text classification is that we have many electronic documents readily available. But, labeling the documents must typically be done by a person, which is a costly and time-consuming process. Nigam et al. showed that, in certain circumstances, it is possible to train a system using both unlabeled and labeled
documents and explained why unlabeled data could benefit the classification task (Nigam, 2001).

3.4.1 The value of unlabeled data

An intuitive idea given by Nigam can make us understand why unlabeled data can be helpful. "Suppose we have some web pages about academic courses, along with a large number of web pages that are unlabeled. By looking at just the labeled data we determine that pages containing the word homework tend to be about academic courses. If we use this fact to estimate the classification of the many unlabeled web pages, we might find that the word lecture occurs frequently in the unlabeled examples that are now believed to belong to the positive class. This co-occurrence of the words homework and lecture over the large set of unlabeled training data can provide useful information to construct a more accurate classifier that considers both homework and lecture as indicators of positive examples" (Nigam, 2001).

3.4.2 Semi-supervised Expectation Maximization with Naive Bayes

The model considered in (Nigam, 2001) uses an algorithm for learning from labeled and unlabeled documents based on the combination of Expectation-Maximization (EM) and the naive Bayes classifier.

When we have unlabeled data available, we would still like to find MAP parameter estimates, as in the supervised setting above. Using the Expectation-Maximization (EM) technique, we can find locally MAP parameter estimates for the generative model.
The probability of an individual unlabeled document is a sum of total probability over all the classes, as in equation 3-3. Hence, the expected log probability of the data, containing $|D|$, is:

$$l(\theta|D,Y) = \log(P(\theta)) + \sum_{i=1}^{[D]} \log \sum_{j=1}^{C} P(c_j|\theta)P(d_i|c_j; \theta)$$ 3-16

The Expectation-Maximization (EM) is a two-step process that provides an iterative approach to finding a local maximum of model probability in parameter space. The E-step of the algorithm estimates the expectations of the class given the latest iteration of the model parameters. The M-step maximizes the likelihood of the model parameters using the previously computed expectations of the missing values as if they were the true ones.

In practice, the E-step corresponds to performing classification of each unlabeled document using equation 3-9. The M-step corresponds to calculating a new maximum a posteriori estimate for the parameters, using Equations 3-7 and 3-8 with the current estimates.

This algorithm is guaranteed to converge to some local maxima. The algorithm iterates until it converges to a point where the parameters does not change from one iteration to the next.

For the semi-supervised case, we consider using a limited number of labeled data in the initialization step. We first train a classifier using the labeled data, and then estimate the parameters. After that, the algorithm iterates trying to improve the log likelihood of the data. The algorithm for the semi-supervised document classification is shown in Figure 3-4.
EM_Semi-supervised_NaiveBayes

Inputs:
D := Collection of labeled documents
D_u := Collection of unlabeled documents

1. Train a classifier with the labeled data and use maximum a posteriori parameter estimation to find θ.
2. Loop while classifier parameters improve, as measured by the change in l(θ|D,Y).
   (E-step) Use the current classifier, θ, to estimate component membership of each document, P(c_j|D_iθ).
   (M-step) Re-estimate the classifier, θ, given the estimated component membership of each document. Use MAP estimation to find θ = arg max P(D,Y|θ)P(θ).

Figure 3-4 Algorithm for the semi-supervised Naïve Bayes document classification using EM

3.4.3 Semi-supervised Probabilistic Latent Semantic Analysis

Probabilistic Latent Semantic Analysis (PLSA) introduced by Hofmann (Hofmann, 1999) has been presented as a probabilistic version of the Latent Semantic Analysis. PLSA algorithm for textual information has the nice property that avoids the ambiguity generated by the words that have synonyms and by the words that are polysems. PLSA tries to find some meaning behind the words, including in the model an unobserved variable representing the topic or aspect. In this model the correspondence between classes and topics is one-to-many (Krithara et al., 2008).

PLSA characterizes each word in a document as a sample form a mixture model, where mixture components are conditionally-independent multinomial distributions.

Let us assume we have a dataset of l labeled documents 
\[ L = \{(x_1, y_1), (x_2, y_2), \ldots (x_l, y_l)\} \] and a dataset of u unlabeled documents
In order to make use of the unlabeled documents, we introduce a "fake" label $z$ for each document, such that $z_i = y_i$ for every labeled document, and $z_i = 0$ for every unlabeled document (Krithara et al., 2006).

In this model, each example $x$ is the co-occurrence of a word $w$ with a document $d$, which we denote $x = (w, d)$. The probabilistic model is a mixture of multinomial distributions over $(w, d, z)$.

$$P(w, d, z) = P(d) \sum_{c=1}^{C} P(w|c)P(c|d)P(z|c)$$  \hspace{1cm} (3-17)

where $C$ is the number of the latent components. Note that they assume that $w, d$ and $z$ are conditionally independent given $c$.

Then, a variant of Expectation-Maximization algorithm is used to train the model. In the Expectation (E) step, we calculate:

$$\pi_c(w, d) = P(c|w, d, z(d)) = \frac{P(c|d)P(w|c)P(z(d)|c)}{\sum_{c'}P(c'|d)P(w|c')P(z(d)|c')}$$  \hspace{1cm} (3-18)

In the Maximization (M) step, the parameters of the model are updated using the following:

$$P(w|c) \propto \sum_d n(w, d)\pi_c(w, d)$$  \hspace{1cm} (3-19)

$$P(c|d) \propto \sum_w n(w, d)\pi_c(w, d)$$  \hspace{1cm} (3-20)
After training the model, the probability obtained for the “fake” label is distributed onto the “real” labels:

\[ P(y|x) \propto P(z = y|x) + \lambda P(y|z = 0)P(z = 0|x) \]  

Where \( \lambda \) is a suitable parameter.

### 3.4.4 Semi-supervised Support Vector Machines

Bennet (Bennett et al., 1998) proposed the semi-supervised Support Vector Machine called S\(^3\)VM. Either formulation given in equation 3-14 or in equation 3-15 could be used as an initial situation. In order to use the unlabeled data, two constraints are added for each point in the working set. One constraint calculates the misclassification error as if the point was in class 1 and the other constraint calculates the misclassification error as if the point was in class -1. The objective function calculates the minimum of the two possible misclassification errors. The class of the points corresponds to the one that results in the smallest error. S\(^3\)VM is defined by the following formulation:

\[
\min_{w,b,\eta,\xi,z} C \left[ \sum_{i=1}^{l} n_i + \sum_{j=l+1}^{l+k} \min(\xi_j, z_j) \right] + ||w||
\]

s.t. \( y_i(w.x_i + b) + n_i \geq 1 \) \( n_i \geq 0, i = 1, \ldots, l \)
Where \( C \) is a positive constant for the misclassification penalty.

The solution of this problem, using integer programming leads to the use of decision variable \( d_j \) for each unlabeled example \( x_j \). This variable indicates the class of the point. If \( d_j = 1 \) then the point is in class 1 and if \( d_j = 0 \) then the point is in class -1. The formulation becomes:

\[
\begin{align*}
\min_{w, b, \eta, \xi, z} & \quad \frac{1}{C} \left[ \sum_{i=1}^{l} n_i + \sum_{j=l+1}^{l+k} \min(\xi_j, z_j) \right] + ||w|| \\
\text{s.t.} & \quad y_i (w.x_i - b) + n_i \geq 1 \\
& \quad w.x_i - b + \xi_j + M \left( 1 - d_j \right) \geq 1 \\
& \quad -(w.x_j - b) + z_j + Md_j \geq 1 \\
& \quad \xi_j \geq 0, j = l + 1, \ldots l + k \\
& \quad z_j \geq 0, \quad d_j = \{0,1\} \\
M & \text{ is a positive constant that is chosen sufficiently large such that if } d_j = 0 \text{ then } \xi_j = 0 \text{ is feasible for any optimal } w \text{ and } b. \text{ Likewise, if } d_j = 1 \text{ then } z_j = 0. \\
\end{align*}
\]

The idea of the use of both labeled and unlabeled with Support Vector Machines is related to the use of transductive inference. We will expand this concept in chapter 4.
3.5 Ontology

The evolution of the web has originated new forms of information sharing. The continuous growing of information in the WWW makes the existence of explicit semantics that supports machine processing of information necessary. The concept of Ontologies was originated in the Artificial Intelligence community as an effort to formalize descriptions of particular domains.

The term 'ontology' in the context of information management is defined as a formal, explicit specification of a shared conceptualization (Gruber, 1993). A conceptualization refers to an abstract model of some phenomenon in the world which identifies the relevant concepts, relations and constraints. These concepts, relations and constraints must be explicitly defined. Formal refers to the fact that the ontology should be machine-readable. Finally, an ontology represents shared knowledge, that is a common understanding of the domain between several parties. Ontologies enable semantic mapping between information sources (Lacy, 2005).

In other words, ontology specifies a domain theory. It is a formal description of concepts and their relations, together with constraints on those concepts and relations. (Alexiev et al., 2005).

It is worth noting that a database schema differs from an ontology given the fact that the last one does not represent shared knowledge. They are typically developed for one or a limited set of applications.
3.5.1 *Types of ontologies*

There are many different types of ontologies. Typically they are classified according to their expressiveness. Alexiev et. al. (Alexiev et al., 2005) classify ontologies into two groups:

1. **Light-weight ontologies.** The ontologies in this group are those with the lower level of expressiveness, they are:
   
   - controled vocabulary: a list of terms.
   - thesaurus: relation between terms are provided.
   - informal taxonomy: there is an explicit hierarchy, but there is not strict inheritance.
   - formal taxonomy: there is strict inheritance.
   - frames or classes: a frame (or class) contains a number of properties and these properties are inherited by subclasses and instances.

2. **Heavy-weight ontologies.**

   1. value restrictions: values of properties are restricted.
   2. general logic constraints: values may be constraint by logical or mathematical formulas.
   3. first-order logic constraints: very expressive ontology languages that allow first-order logic constraints between terms and more detailed relationships such as disjoint
classes, disjoint coverings, inverse relationships, part-whole relationships, etc. feasible for any optimal $w$ and $b$. Likewise if $d_j = 1$ then $z_j = 0$.

### 3.5.2 Examples of ontologies

Currently, there exist many published ontologies, some of them are listed below:

- **WordNet** (Princeton University, 2010), a lexical reference system.
- **Opencyc** (Cycorp, 2011), a large Foundation Ontology for formal representation of the universe of discourse.
- **Gene Ontology for genomics** (IFOMIS, 2011).
- **CContology** (Jarrar, 2007). Customer Complaint Ontology, an e-business ontology to support online customer complaint management.
- **BMO** (Jenz & Partner), an e-Business Model Ontology based on a review of enterprise ontologies and business model literature.
- **COSMO** (MICRA, 2011), a Foundation Ontology that is designed to contain representations of all of the primitive concepts needed to logically specify the meanings of any domain entity. It is intended to serve as a basic ontology that can be used to translate among the representations in other ontologies or databases.
- **DOLCE** (LOA, 2006), a Descriptive Ontology for Linguistic and Cognitive Engineering.
- **Dublin Core** (University of Maryland, 2000), a simple ontology for documents and publishing.
- Foundational Model of Anatomy (University of Washington, 2011), an ontology for human anatomy.

    In addition, semantic web search engines have also been developed. Some of them are Swoogle (UMBC, 2007) and SWSE (SWSE, 2010) (pronounced "swizzy").

    In this thesis, we have mainly used Wordnet (Princeton University, 2010), Opencyc (Cycorp, 2011) and other ontologies found using the semantic web search engine Swoogle (UMBC, 2007).
4 SEMI-SUPERVISED SUPPORT VECTOR MACHINES USING ONTOLOGIES

4.1 Transductive Support Vector Machines (TSVM)

Transductive learning refers to the estimation of the class of the unlabeled working set. In contrast with the inductive approach where the learner induces a function with low error rate; transductive learning aims to classify a given set of unlabeled examples with as few errors as possible. The most representative technique of transductive learning is Transductive Support Vector Machines (TSVM). It was introduced by Joachims (Joachims, 1999) with particular application in Text Classification.

TSVM maximizes margin not only on the training, but also on the test set. For transductive learning, the learner L receives as input a training set \( S = \{ (x_1, y_1), (x_2, y_2), ..., (x_l, y_l) \} \) and a test set \( T = \{ x_1^*, x_2^*, ..., x_k^* \} \) (from the same distribution) (Joachims, 1999).

Including \( T = \{ x_1^*, x_2^*, ..., x_k^* \} \), the corresponding labeling \( y_1^*, y_2^*, ..., y_k^* \) to be found and the slack variables \( \xi_j^*, j = 1, ..., k \) for the unlabeled data in the derivation, we arrive to the following optimization problem for the non-separable case:
\[
\begin{align*}
\text{min: } & W(y_1^*, y_2^*, ..., y_n^*, w, b, \xi_1, ..., \xi_k) = \frac{1}{2} \|w\| + C \sum_{i=0}^{n} \xi_i + C^* \sum_{j=0}^{k} \xi_j^* \\
\text{s.t.} & \quad (w \cdot x_i + b) \geq 1 - \xi_i \\
& \quad y_j^* (w \cdot x_j^* + b) \geq 1 - \xi_j^* \\
& \quad y_j^* \in \{-1, 1\} \\
& \quad \xi_i \geq 0, i = 1, ... n \\
& \quad \xi_j^* \geq 0, j = 1, ... k \\
\end{align*}
\]

\(C\) and \(C^*\) are parameters set by the user. They allow trading off margin size against misclassifying training examples or excluding test examples.

Solving this problem means finding a labeling \(y_1^*, y_2^*, ..., y_n^*\) of the test data and a hyperplane \(\langle w, b \rangle\), so that this hyperplane separates both training and test data with maximum margin.

For a very small number of test examples, this problem can be solved simply by trying all possible assignments of \(y_1^*, y_2^*, ..., y_n^*\) to the two classes. However, this approach becomes intractable for large test sets. (Joachims, 2001), proposed an algorithm that repeatedly optimize approximations to the TSVM training problem using local search. Local search algorithms start with some initial instantiation of the variables. In each iteration the current variable instantiation is modified so that it moves closer to a solution. This process is iterated until no more improvement is possible.
Figure 4-1 Example of the influence of unlabeled examples in TSVM.

An intuitive graphical interpretation explaining how TSVM works is shown in Figure 4-1. Plus signs indicate positive examples; minus signs indicate negative examples and dots stand for unlabeled examples. In part (a) the dashed line indicates the hyperplane with the maximum margin when no unlabeled examples are taken into account. In part (b) the solid line represents the hyperplane with the maximum margin when unlabeled examples are taken into account.

The algorithm proposed by (Joachims, 2001) is shown in Figure 4-2. The algorithm takes the training data and the test examples as input. The user can specify the number of test examples to be assigned to the positive class. This version of the algorithm covers the linear case. It could be easily adapted for the use of kernels.

At each level of approximation, the algorithm improves the solution by switching the labels of a pair of test examples. The criterion in the condition of loop 2 identifies two examples for which changing the class labels leads to a decrease in the current objective.
function. If there are no more such examples, the algorithm moves to a closer approximation in loop 1. The function \textit{solve_svm_qp} is used as a sub procedure that solves the optimization problem 4.1, it uses the current solution as a starting point.

This algorithm is guaranteed to converge as proved by (Joachims, 2001). He also states that the algorithm was empirically found to be robust against getting stuck in local minima far away from the optimum.

\begin{algorithm}
\textbf{ALGORITHM TSVM}

\begin{enumerate}
\item Train an inductive SVM \( M_1 \) using the labeled data \((x_1, y_1), ..., (x_n, y_n)\).
\item Classify unlabeled documents \( x_1^*, ..., x_k^* \) using \( M_1 \)
\item Loop 1: While there exist unlabeled documents
  \begin{enumerate}
  \item Increase the influence of unlabeled data by incrementing the cost factors (parameters in the algorithm)
  \item Loop 2: While there exist unlabeled examples that do not meet the restriction of the optimization problem
    \begin{enumerate}
    \item Improve the solution by switching the labels of a pair of unlabeled examples
    \item Retrain
    \end{enumerate}
  \end{enumerate}
\item Return labels \( y_1^*, ..., y_k^* \) for unlabeled documents
\end{enumerate}
\end{algorithm}

\textbf{Figure 4-2 Algorithm for training TSV} (Joachims, 1999)
4.2 Incorporating ontologies to TSVM

Given a collection of ontologies related to the classification problem, we build a vector of the form:

\[ v_{ont} = (x_i, y_i), i = 1, ..., c \]

where \( c \) is the number of classes in the classification problem. Each \( x_i \) is a vector of words that are known to be good discriminator for class \( y_i \).

Additionally, to each word could be associated a weight \( w_j \) that corresponds to the importance of word \( x_j \) in discriminating its corresponding class.

For this work we focus our attention in binary classification, hence the set of classes will be \( \{1, -1\} \)

Our proposal is to incorporate the ontologies in the algorithm, in order to use this information to help make the decision of which unlabeled examples are worth switch to labeled samples. We use the information of a probabilistic label given to each unlabeled document by the ontologies. The intention is not to push too hard to conform strictly to the ontologies, but use it as a piece of information in that point of the algorithm.

In order to use the information provided by the ontology, we first assign to each unlabeled document \( d^* \) a probabilistic label \( z \) induced by the ontologies.
Let \( \mathbf{d} = (w_1, w_2, \ldots, w_k) \) be a document, and let \( \{(a_1, a_2, \ldots, a_p, +1), (b_1, b_2, \ldots, b_n, -1)\} \) be the ontology for a binary problem.

Then we assign to the unlabeled document \( \mathbf{d} \) a label \( y_{ont} \) using the following rule:

\[
y_{ont} = \arg\max_i \left( \sum_{w_j \in \mathbf{v}_{ont_i}} w_j \right)
\]

The algorithm for assigning the labels induced by ontologies is shown in Figure 4-3.

```
ALGORITHM ONTOLOGY_LABEL

Input: training examples \( x_1, \ldots, x_k \)
ontology \( \{(a_1, a_2, \ldots, a_p, +1), (b_1, b_2, \ldots, b_n, -1)\} \)

Output Probabilistic labels of the test examples \( z_1^*, \ldots, z_k^* \)

//Words are ordered by id in both document vectors and ontology vectors
// Repeat for all unlabeled examples
for (i = 0, i < k, i += 1)
    posweight := 0
    negweight := 0

    for (j = 0, j < p, j += 1)
        if (a_j \in x_i^*) \{ posweight := posweight + weight(x \in x_i^*|x = a_j) \}

    for (j = 0, j < n, j += 1)
        if (b_j \in x_i^*) \{ negweight := negweight + weight(x \in x_i^*|x = b_j) \}

    \( y_{ont_i} := \max(posweight, negweight) \)
    If (posweight < negweight) \( y_{ont_i} := -y_{ont_i} \)

Figure 4-3 Algorithm for calculating the label induced by the Ontology
```
For weighted ontologies, we just multiply corresponding weights of document word and ontology word.

Once we have obtained the probabilistic label for all unlabeled documents, we can make the following modification in the transductive approach shown in section 4.1.

\[
\text{ALGORITHM TSVM}
\]

\begin{itemize}
  \item Input: labeled examples \((x_1, y_1), \ldots, (x_n, y_n)\)
  \item unlabeled examples \(x_1^*, \ldots, x_k^*\)
  \item labels induced by ontologies \(z_1^*, \ldots, z_k^*\) for unlabeled documents
\end{itemize}

\begin{itemize}
  \item Output: Predicted labels of the unlabeled examples \(y_1^*, \ldots, y_k^*\)
  \item 1. Train an inductive SVM \(M_1\) using the labeled data \((x_1, y_1), \ldots, (x_n, y_n)\).
  \item 2. Classify unlabeled documents \(x_1^*, \ldots, x_k^*\) using \(M_1\).
  \item 3. Loop 1: While there exist unlabeled documents
    \begin{itemize}
      \item 3. Increase the influence of unlabeled data by incrementing the cost factors (parameters in the algorithm)
      \item 4. Loop 2: While there exist unlabeled examples that do not meet the restriction of the optimization problem
        \begin{itemize}
          \item 3. Select unlabeled examples to switch given that are misclassified according to the ontology induced label \(z_1^*, \ldots, z_k^*\)
          \item 4. Retrain
        \end{itemize}
    \end{itemize}
  \item 4. Return labels \(y_1^*, \ldots, y_k^*\) for unlabeled documents
\end{itemize}

\textbf{Figure 4-4 Algorithm for training transductive support vector machines using ontologies.}
A graphical interpretation of this algorithm could be seen in Figure 2-1, (a) in any iteration, the algorithm decides to make a switch between the examples that are closer to the margin. In this case we can also make use of the probabilistic label of the unlabeled example (label 0.8) to decide that this example is likely to be positive. (b) The new separating hyperplane is shown in purple.

Figure 4-5 Graphical interpretation of the use of labels induced by ontologies.

4.3 Justification for using Ontologies

The reasons for incorporating ontologies to our model are:

1. We could easily get the ontologies vectors. The manual construction of these vectors does not represent a significant cost in human effort, since extracting the keywords from ontologies for each class is easy than read and label thousands of documents.
2. We can guide the classification task for the unlabeled data in a desired direction, since we can give specific words for a class, and we can even assign weights to them. Depending on the problem, this could be desirable.

4.4 Time Complexity of the Algorithm

Using the sparse vector representation the time complexity of the dot products depend only on the number of non-zero entries.

Let $m$ the maximum number of non-zero entries in any of the training examples, let $q$ be the rows of the Hessian. For each iteration, most time is spent on the Kernel evaluations needed to compute the Hessian. Since we used a linear Kernel, this step has time complexity $O(q^2 m)$.

4.5 Related work

Traditionally, ontologies were used to help pre-processing text documents, such as the use of WordNet to find synonyms to be considered as one word or token.

A distinct approach is presented in (Carlson, 2010). He extracts facts and relationships from the web and builds ontologies. He uses these ontologies as constraints to learn semi-supervised functions at one in a coupled manner.

Recently, (Chenthamarakshan et al., 2011) present an approach in which they first map concepts in an ontology to the target classes of interest. They label unlabeled examples
using this mapping, in order to use them as training set for any classifier. They called this process concept labeling.
5 EXPERIMENTAL EVALUATION

5.1 Datasets

We used three well known data sets among researchers in text mining and information retrieval. These datasets are described below.

*Reuters-1 (RCV1)*

In 2000, Reuters Ltd. made available a large collection of Reuters News stories for use in research and development of natural language processing, information retrieval, and machine learning systems. This corpus, known as "Reuters Corpus, Volume 1" or RCV1, is significantly larger than the older, well-known Reuters-21578 collection heavily used in the text classification community. This is distributed on two CDs and contains about 810,000 Reuters, English Language News stories. It requires about 2.5 GB for storage of the uncompressed files.

In Fall of 2004, NIST took over distribution of RCV1 and any future Reuters Corpora. These datasets can be obtained from NIST upon request.

This data set is described in detail by Lewis et. al. (Lewis et al., 2004). In this thesis, we randomly selected a portion of documents from the most populated categories. The quantity of selected documents is proportional to the total amount of documents in each category. In Table 5-1, we show the quantity of selected documents, for each category. For the negative class of each category, we randomly selected the same amount of documents from the other categories.
<table>
<thead>
<tr>
<th>CATEGORY</th>
<th>LABELED</th>
<th>UNLABELED</th>
<th>TOTAL</th>
</tr>
</thead>
<tbody>
<tr>
<td>Accounts/earnings</td>
<td>1325</td>
<td>25069</td>
<td>26394</td>
</tr>
<tr>
<td>Equity markets</td>
<td>1048</td>
<td>20296</td>
<td>21344</td>
</tr>
<tr>
<td>Mergers/acquisitions</td>
<td>960</td>
<td>18430</td>
<td>19390</td>
</tr>
<tr>
<td>Sports</td>
<td>813</td>
<td>15260</td>
<td>16073</td>
</tr>
<tr>
<td>Domestic politics</td>
<td>582</td>
<td>11291</td>
<td>11873</td>
</tr>
<tr>
<td>War, civil war</td>
<td>1001</td>
<td>17652</td>
<td>18653</td>
</tr>
<tr>
<td>Crime, law enforcement</td>
<td>466</td>
<td>7205</td>
<td>7671</td>
</tr>
<tr>
<td>Labour issues</td>
<td>230</td>
<td>6396</td>
<td>6626</td>
</tr>
<tr>
<td>Metals trading</td>
<td>505</td>
<td>9025</td>
<td>9530</td>
</tr>
<tr>
<td>Monetary/economic</td>
<td>533</td>
<td>5663</td>
<td>6196</td>
</tr>
</tbody>
</table>

Table 5-1 Number of labeled and unlabeled documents used in experiments for 10 categories of Reuters dataset.

20 Newsgroups

The 20 Newsgroups data set was collected by Ken Lang, consists of 20017 articles divided almost evenly among 20 different UseNet discussion groups.

Some of the newsgroups are very closely related to each other (e.g. comp.sys.ibm.pc.hardware / comp.sys.mac.hardware), while others are highly unrelated (e.g. misc.forsale / soc.religion.christian). Here is the list of the 20 newsgroups:

- comp.graphics
- comp.os.ms-windows.misc
- comp.sys.ibm.pc.hardware
- comp.sys.mac.hardware
- comp.windows.x.
- rec.autos
- rec.motorcycles
- rec.sport.baseball
- rec.sport.hockey
- sci.crypt
- sci.electronics
- sci.med
- sci.space
- talk.politics.misc
- talk.politics.guns
- talk.politics.mideast
- talk.religion.misc
- alt.atheism
- soc.religion.christian
- misc.forsalehre
This data set is available from many online data archives such as CMU Machine Learning Repository (UCI, 2011).

For our experiments we used 10000 documents corresponding to 10 categories. For each class we used 100 labeled documents and 900 unlabeled documents.

**WebKB**

The WebKB data set described at (Craven et al., 1998) contains 8145 web pages gathered from universities computer science departments. The collection includes the entirety of four departments, and additionally, an assortment of pages from other universities. The pages are divided into seven categories: student, faculty, staff, course, project, department and other.

In this thesis, we used the four most populous categories (excluding the category other): student, faculty, course and project. A total of 4199 pages, distributed in the following way:

<table>
<thead>
<tr>
<th>CATEGORY</th>
<th>LABELED</th>
<th>UNLABELED</th>
<th>TOTAL</th>
</tr>
</thead>
<tbody>
<tr>
<td>Course</td>
<td>93</td>
<td>837</td>
<td>930</td>
</tr>
<tr>
<td>Department</td>
<td>18</td>
<td>164</td>
<td>182</td>
</tr>
<tr>
<td>Faculty</td>
<td>112</td>
<td>1012</td>
<td>1124</td>
</tr>
<tr>
<td>Student</td>
<td>164</td>
<td>1477</td>
<td>1641</td>
</tr>
</tbody>
</table>

Table 5-2 Number of labeled and unlabeled documents used in experiments for 4 categories of Web-Kb dataset.
5.2 Ontologies

The keywords for the ontology vectors for each class were collected mainly from
Wordnet, Opencyc, among other ontologies, provided by the semantic browser swoogle,
depending on the class of interest.

5.3 Performance measures

In order to evaluate and compare the classifiers, we used the most common
performance measures, which we describe below. The estimators for these measures can be
defined based on the following contingency table:

<table>
<thead>
<tr>
<th>Prediction $f(x) = +1$</th>
<th>Label $y = +1$</th>
<th>Label $y = -1$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Prediction $f(x) = -1$</td>
<td>$PP$</td>
<td>$PN$</td>
</tr>
<tr>
<td></td>
<td>$NP$</td>
<td>$NN$</td>
</tr>
</tbody>
</table>

Table 5.3 Contingency table for binary classification.

Each cell of the table represents one of the four possible outcomes of a prediction
$f(x)$ for an example $(x,y)$.

5.3.1 Error rate and Accuracy

Error rate is probability that the classification function $f$ predicts the wrong class.

$$Err(f) = \Pr(f(x) \neq y|f)$$

It can be estimated as:

$$Err(f) = \frac{PN + NP}{PP + PN + NP + NN}$$
Accuracy measures the ratio of correct predictions to the total number of cases evaluated.

\[ A(f) = \frac{PP + NN}{PP + PN + NP + NN} \]

5.3.2 Asymmetric cost

In text classification problems usually negative examples exceed positive examples. For this reason, error rate is not always a good performance measure for text classification. Moreover, for many applications, predicting a positive example correctly is more important than predicting a negative example correctly. For this reason this measure considers a cost weight \( C_i \) for the values in the contingency Table 5-3.

\[ Cost_{test}(f) = \frac{C_{pp}PP + C_{pn}PN + C_{np}NP + C_{nn}NN}{PP + PN + NP + NN} \]

5.3.3 Recall

Recall is defined as the probability that a document with label \( y = 1 \) is classified correctly. It could be estimated as follows:

\[ Rec_{test}(f) = \frac{PP}{PP + NP} \]

5.3.4 Precision

Precision is defined as the probability that a document classified as \( f(x) = 1 \) is classified correctly. It could be estimated as follows

\[ Prec_{test}(f) = \frac{PP}{PP + PN} \]
5.3.5 Precision / Recall breakeven point and $F_\beta$-Measure

Precision and recall are combined to give a single measure, to make it easier to compare learning algorithms.

$F_\beta$-Measure is the weighted harmonic mean of precision and recall. It can be estimated from the contingency table as:

$$F_{\beta, test}(f) = \frac{(1 + \beta^2)PP}{(1 + \beta^2)PP + PN + \beta^2NP}$$

Precision / Recall breakeven point (PRBEP) is the value at which precision and recall are equal. $\beta$ is a parameter. The most commonly used value is $\beta = 1$, giving equal weight to precision and recall.

5.4 Design Considerations

Preprocessing

- We created a sparse vector representation of the documents, using normalized term frequency.
- The data sets were preprocessed to remove stop words.
- Additionally, low-frequency words appearing in less than 0.2% of the documents, were eliminated.

Implementation

- Our algorithms are suited to use a sparse vector representation of documents.

Evaluation
• Accuracy, Precision and Recall are used as evaluation measure.

5.5 Implementation

5.5.1 Sparse Representation

Let \( d \) the number of documents in the collection \( D \) and \( |V| \) the total number of different words (i.e. the vocabulary length). In order to store the document vectors, we should need a matrix of order \( O(d|V|) \).

However, most documents contain a small subset of the dictionary's words. In the case of text classification, a text corpus might have thousands of word types. Each individual document, however, has only a few hundred unique tokens. So, in the numerical vectors, almost all of the entries for that document will be zero. Rather than store all the zeros, it is better to represent the matrix as a set of sparse vectors, where a row is represented by a list of pairs, one element of the pair being a column number and the other element being the corresponding nonzero feature value. By not storing the zeros, savings in memory can be immense. Processing programs can be adapted to handle this format.

In this thesis, we store a sparse representation of the vectors. They are stored in text files with the form:

\[
label \ ont\_label \ w_1:weight_1 \ w_2:weight_2 \ w_k:weight_k
\]

Each line in the text document corresponds to a document vector. Label contains the document label for labeled documents and 0 for unlabeled documents, ont_label contains the label obtained from the ontologies.
Then we have a sequence of pairs word id : weight. Weight is the value that corresponds to the word for the current document. This weight could be gotten following any of the weighting schemes sawn in section 2.2.5.

Let $m$ be the non zero weight values of the entire collection. With this representation, the storage growth is in the order of $O(dm)$ which is more efficient than storing all the matrix, since in this sparse context we have that $dm << d*|V|$.

We also use a sparse representation of the ontologies in the same way that the representation used for the document vectors.

For binary classification, let $p$ and $n$ be the number of words extracted from ontologies for the positive class and the negative class respectively, the vectors for the ontologies are of the form:

$$+1 \ w_1, w_2, \ldots, w_p$$
$$-1 \ v_1, v_2, \ldots, v_n$$

They could also include a weight:

$$+1 \ w_1{:weight}, w_2{:weight}, \ldots, w_p{:weight}$$
$$-1 \ v_1{:weight}, v_2{:weight}, \ldots, v_n{:weight}$$

where $weight_i$ indicates a importance measure of a word $w_i$ corresponding to a class.

5.5.2 Implementation of the ontology label calculation

We use ordered list of words in order to make the algorithm efficient. In the preprocessing step, we keep the same order in words for the ontologies than we used for the
document vectors. In a similar way than the merge part of the merge sort algorithm, we pass through the ordered lists once.

5.5.3 Implementation of the TSVM using ontologies

We make use of a very efficient implementation of the SVM algorithm called SVM$^\text{light}$ (Joachims, 1999) in order to benefit from the great characteristics that make this algorithm computationally efficient.

The algorithm is implemented using C programming language and it has great optimizations such as the use of working sets, shrinking of variables and caching Kernel evaluations. The technique of caching the Kernel evaluations consists in keeping in a buffer the calculations for the most frequent support vectors.

5.6 Experimental results

The experiments evaluate the quality and efficiency of the algorithm. The number of documents used, and the splitting of each dataset is described in section 5.1.

For Twenty newsgroups dataset, the experiments are shown in Table 5-4, for selected 10 categories. Each category consists of 2000 examples from which 10 percent are labeled documents. In this table we can see an improvement with respect to the TSVM in the accuracy for three categories. The highest improvement is reached for category soc.religion.christian. Table 5-5 shows the values of precision and recall for the same dataset. In
In this table we note that precision improves in all cases in which accuracy has been improved by the use of ontologies.

We also note that in two cases there has been a little lost in accuracy by the use of ontologies. We conjecture that the reason is that the selected ontologies might not agree with the manual labeling.

<table>
<thead>
<tr>
<th>CATEGORY</th>
<th>TSVM</th>
<th>TSVM+ONT</th>
<th>GAIN</th>
</tr>
</thead>
<tbody>
<tr>
<td>alt.atheism</td>
<td>81.25</td>
<td>88.12</td>
<td>6.87</td>
</tr>
<tr>
<td>comp.graphics</td>
<td>93.67</td>
<td>94.3</td>
<td>0.63</td>
</tr>
<tr>
<td>misc.forsale</td>
<td>89.38</td>
<td>94.38</td>
<td>5</td>
</tr>
<tr>
<td>rec.autos</td>
<td>77.36</td>
<td>76.1</td>
<td>-1.26</td>
</tr>
<tr>
<td>rec.motorcycles</td>
<td>74.68</td>
<td>74.68</td>
<td>0</td>
</tr>
<tr>
<td>sci.electronics</td>
<td>66.88</td>
<td>66.88</td>
<td>0</td>
</tr>
<tr>
<td>sci.med</td>
<td>75.32</td>
<td>74.68</td>
<td>-0.64</td>
</tr>
<tr>
<td>soc.religion.christian</td>
<td>73.58</td>
<td>94.34</td>
<td>20.76</td>
</tr>
<tr>
<td>talk.politics.guns</td>
<td>97.45</td>
<td>97.45</td>
<td>0</td>
</tr>
<tr>
<td>rec.sport.baseball</td>
<td>86.16</td>
<td>86.16</td>
<td>0</td>
</tr>
</tbody>
</table>

Table 5-4 Accuracy of TSVM y TSVM + ontologies for ten categories of Twenty Newsgroups.

<table>
<thead>
<tr>
<th>CATEGORY</th>
<th>TSVM</th>
<th>TSVM+ONT</th>
</tr>
</thead>
<tbody>
<tr>
<td>alt.atheism</td>
<td>71.15%/100.00%</td>
<td>80.90%/97.30%</td>
</tr>
<tr>
<td>comp.graphics</td>
<td>88.51%/100.00%</td>
<td>89.53%/100.00%</td>
</tr>
<tr>
<td>misc.forsale</td>
<td>82.61%/98.70%</td>
<td>91.46%/97.40%</td>
</tr>
<tr>
<td>rec.autos</td>
<td>96.30%/60.47%</td>
<td>96.15%/58.14%</td>
</tr>
<tr>
<td>rec.motorcycles</td>
<td>96.08%/56.32%</td>
<td>96.08%/56.32%</td>
</tr>
<tr>
<td>sci.electronics</td>
<td>90.91%/44.94%</td>
<td>90.91%/44.94%</td>
</tr>
<tr>
<td>sci.med</td>
<td>91.07%/60.00%</td>
<td>90.91%/58.82%</td>
</tr>
<tr>
<td>soc.religion.christian</td>
<td>62.73%/98.57%</td>
<td>89.61%/98.57%</td>
</tr>
<tr>
<td>talk.politics.guns</td>
<td>96.25%/98.72%</td>
<td>96.25%/98.72%</td>
</tr>
<tr>
<td>rec.sport.baseball</td>
<td>100.00%/73.81%</td>
<td>100.00%/73.81%</td>
</tr>
</tbody>
</table>

Table 5-5 Precision and Recall of TSVM y TSVM + ontologies for ten categories of Twenty Newsgroups.
For Web-Kb dataset, the experiments are shown in Table 5-6, for the four categories that are commonly used by researchers (Nigam et al., 1998), (Joachims, 2001). We use all the available documents for each category. Ten percent of the documents were labeled and the rest was selected as unlabeled documents. In Table 5-6 we can see an improvement in the accuracy for three categories. Table 5-7 shows the precision and recall measures for Web-Kb dataset. This table shows an increment in precision even in the category in which ontologies do not report an improvement in comparison with TSVM.

<table>
<thead>
<tr>
<th>CATEGORY</th>
<th>TSVM</th>
<th>TSV+ONT</th>
<th>GAIN</th>
</tr>
</thead>
<tbody>
<tr>
<td>Course</td>
<td>96.5</td>
<td>96.84</td>
<td>0.34</td>
</tr>
<tr>
<td>Department</td>
<td>93.48</td>
<td>94.6</td>
<td>1.12</td>
</tr>
<tr>
<td>Faculty</td>
<td>85.29</td>
<td>84.8</td>
<td>-0.49</td>
</tr>
<tr>
<td>Student</td>
<td>83.94</td>
<td>84.34</td>
<td>0.4</td>
</tr>
</tbody>
</table>

Table 5-6 Accuracy of TSVM y TSVM + ontologies for 4 categories of Web-Kb dataset.

<table>
<thead>
<tr>
<th>CATEGORY</th>
<th>TSVM</th>
<th>TSV+ONT</th>
</tr>
</thead>
<tbody>
<tr>
<td>Course</td>
<td>97.05%/98.77%</td>
<td>97.70%/98.50%</td>
</tr>
<tr>
<td>Department</td>
<td>74.85%/88.65%</td>
<td>81.63%/85.11%</td>
</tr>
<tr>
<td>Faculty</td>
<td>90.22%/73.13%</td>
<td>90.96%/71.09%</td>
</tr>
<tr>
<td>Student</td>
<td>86.20%/86.79%</td>
<td>87.66%/85.65%</td>
</tr>
</tbody>
</table>

Table 5-7 Precision and Recall of TSVM y TSVM + ontologies for 4 categories of Web-Kb dataset.

The third set of experiments corresponds to Reuters dataset, and are shown in Table 5-8. We selected a sample for the ten most populated categories. In this table we can see an improvement in the accuracy in nine of the ten selected categories. There is no lost reported in any of the categories. Table 5-9 shows the corresponding precision and recall measures for this experiment. We note again an increment in precision for all categories. With this dataset...
it was easier to find related ontologies since categories are well defined. This might be the
reason why ontologies were beneficial in nine categories and had no effect in just one
category.

<table>
<thead>
<tr>
<th>CATEGORY</th>
<th>TSVM</th>
<th>TSV+ONT</th>
<th>GAIN</th>
</tr>
</thead>
<tbody>
<tr>
<td>Accounts/earnings</td>
<td>96.30</td>
<td>96.45</td>
<td>0.15</td>
</tr>
<tr>
<td>Equity markets</td>
<td>92.5</td>
<td>93.7</td>
<td>1.20</td>
</tr>
<tr>
<td>Mergers/acquisitions</td>
<td>96.2</td>
<td>96.4</td>
<td>0.20</td>
</tr>
<tr>
<td>Sports</td>
<td>96.46</td>
<td>96.46</td>
<td>0.00</td>
</tr>
<tr>
<td>Domestic politics</td>
<td>83.4</td>
<td>83.9</td>
<td>0.50</td>
</tr>
<tr>
<td>War, civil war</td>
<td>94.06</td>
<td>95.98</td>
<td>1.92</td>
</tr>
<tr>
<td>Crime, law enforcement</td>
<td>92.7</td>
<td>95.14</td>
<td>2.44</td>
</tr>
<tr>
<td>Labour issues</td>
<td>85.5</td>
<td>87.15</td>
<td>1.65</td>
</tr>
<tr>
<td>Metals trading</td>
<td>96.2</td>
<td>97.48</td>
<td>1.28</td>
</tr>
<tr>
<td>Monetary/economic</td>
<td>85.2</td>
<td>89.7</td>
<td>4.50</td>
</tr>
</tbody>
</table>

Table 5-8 Accuracy of TSVM y TSVM + ontologies for 10 categories of Reuters dataset.

<table>
<thead>
<tr>
<th>CATEGORY</th>
<th>TSVM</th>
<th>TSV+ONT</th>
</tr>
</thead>
<tbody>
<tr>
<td>Accounts/earnings</td>
<td>96.30%/96.30%</td>
<td>97.16%/95.70%</td>
</tr>
<tr>
<td>Equity markets</td>
<td>92.50%/92.50%</td>
<td>93.71%/92.20%</td>
</tr>
<tr>
<td>Mergers/acquisitions</td>
<td>96.20%/96.20%</td>
<td>97.74%/95.00%</td>
</tr>
<tr>
<td>Sports</td>
<td>100.00%/94.06%</td>
<td>100.00%/94.06%</td>
</tr>
<tr>
<td>Domestic politics</td>
<td>83.40%/83.40%</td>
<td>85.61%/81.50%</td>
</tr>
<tr>
<td>War, civil war</td>
<td>89.11%/99.96%</td>
<td>92.37%/99.95%</td>
</tr>
<tr>
<td>Crime, law enforcement</td>
<td>89.20%/99.99%</td>
<td>92.54%/100.00%</td>
</tr>
<tr>
<td>Labour issues</td>
<td>85.50%/85.50%</td>
<td>86.88%/88.10%</td>
</tr>
<tr>
<td>Metals trading</td>
<td>96.20%/96.20%</td>
<td>99.96%/92.09%</td>
</tr>
<tr>
<td>Monetary/economic</td>
<td>85.20%/85.20%</td>
<td>95.21%/81.80%</td>
</tr>
</tbody>
</table>

Table 5-9 Precision and Recall of TSVM y TSVM + ontologies for 10 categories of Reuters dataset.
5.6.1 Influence of the ontologies

Figure 5-1 shows the effect of using ontologies for class soc.religion.christian of Twenty Newsgroups dataset. For a total of 2000 documents, we vary the size of the labeled documents.

![Graph showing accuracy of TSVM and TSVM using ontologies for one class of 20 Newsgroups for 2000 documents varying the amount of labeled documents.](image)

In this particular case, the use of ontologies was equivalent to using about twenty percent more of labeled data (400 labeled documents).

5.6.2 Time efficiency

In Table 5-10, we present the training times in cpu-seconds for both TSVM and TSVM + ontologies for different datasets sizes. We conduct our experiments in a Dell Precision Workstation 650 with Intel Xeon dual processor, 2.80GHz. It has a 533MHz front side bus, a 512K cache and 4GB SDRAM memory at 266MHz.
We note that there is no significant overhead of the use of the ontologies.

<table>
<thead>
<tr>
<th>LABELED</th>
<th>UNLABELED</th>
<th>TOTAL</th>
<th>TSV(s)</th>
<th>TSV+ONT (s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>10</td>
<td>100</td>
<td>110</td>
<td>0.05</td>
<td>0.04</td>
</tr>
<tr>
<td>50</td>
<td>500</td>
<td>550</td>
<td>0.09</td>
<td>0.07</td>
</tr>
<tr>
<td>100</td>
<td>1000</td>
<td>1100</td>
<td>0.14</td>
<td>0.15</td>
</tr>
<tr>
<td>200</td>
<td>2000</td>
<td>2200</td>
<td>7.37</td>
<td>7.19</td>
</tr>
<tr>
<td>500</td>
<td>5000</td>
<td>5500</td>
<td>315.48</td>
<td>471.85</td>
</tr>
<tr>
<td>1000</td>
<td>10000</td>
<td>11000</td>
<td>1162.63</td>
<td>1121.65</td>
</tr>
</tbody>
</table>

Table 5-10 Training time in seconds for different dataset sizes.

Figure 5-2, shows the variation of the training time in cpu-seconds, in logarithmic scale, with respect to the number of documents for the two algorithms. As we can note, there is no substantial difference between them. In some cases, TSVM + ontologies performs better. This could be due the reduction in the number of iterations when we use ontologies as shown in Table 5-11.

Figure 5-2 Training time of TSVM and TSVM using ontologies for different documents sizes.
<table>
<thead>
<tr>
<th>LABELED</th>
<th>UNLABELED</th>
<th>TOTAL</th>
<th>TSV(s)</th>
<th>TSV+ONT (s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>10</td>
<td>100</td>
<td>110</td>
<td>0.05</td>
<td>0.04</td>
</tr>
<tr>
<td>50</td>
<td>500</td>
<td>550</td>
<td>0.09</td>
<td>0.07</td>
</tr>
<tr>
<td>100</td>
<td>1000</td>
<td>1100</td>
<td>0.14</td>
<td>0.15</td>
</tr>
<tr>
<td>200</td>
<td>2000</td>
<td>2200</td>
<td>7.37</td>
<td>7.19</td>
</tr>
<tr>
<td>500</td>
<td>5000</td>
<td>5500</td>
<td>315.48</td>
<td>471.85</td>
</tr>
<tr>
<td>1000</td>
<td>10000</td>
<td>11000</td>
<td>1162.63</td>
<td>1121.65</td>
</tr>
</tbody>
</table>

Table 5-11 Number of iterations for different dataset sizes.
6 CONCLUSIONS AND FUTURE WORK

In this thesis, we studied and implemented the use of ontologies to help the semi-supervised document classification task. We compared the performance of these algorithms in three benchmark data sets: 20 Newsgroups, Reuters and WebKb.

Our experiments improve the accuracy of TSVM in many cases. For twenty newsgroups datasets, we obtain the best results having an improvement up to 20 percent.

We note that precision improves in all cases in which accuracy has been improved by the use of ontologies. Furthermore, we improve precision in almost all cases even in the categories in which ontologies do not report an improvement in comparison with TSVM.

We have shown that the influence of ontologies in some cases reached up to 20 percent of data which in our particular experiment it was equivalent to using about 400 labeled documents.

We also evaluate the time performance. Experimental evaluations show that the running time of the learning TSVM algorithm is not significantly affected by the use of the ontologies in most cases.

We show that we can benefit from domain knowledge, where experts create ontologies in order to guide the direction of the semi-supervised learning algorithm. We also have suggested a way to determine if the available ontologies will benefit the semi-supervised process. In that way, if it is not, one can always select other ontologies.
Ontologies represent a new source of reliable and structured information that can be used at different levels in the process of classifying documents, and this concept can be extended to the use of ontologies in other areas.

Among future work that can be done based on this thesis are:

1. Include other kinds of ontologies in the process of semi-supervised learning. For example, consider first-order logic constraints ontologies in order to incorporate the constraints to the algorithms.

2. Identify the kernels that are well suited for document classification.

3. Design learning algorithms that work efficiently for multiclass settings, and make use of ontologies.

4. For multiclass settings, develop a parallel algorithm in which any slave make a binary classification.
7 ETHICAL CONSIDERATIONS

It is essential that fundamental ethical principles be applied in the design and implementation of scientific research. The principles of research ethics have grown out of abuses in the past. Since its formalization by the declaration of Helsinki in 1974, which current version can be found at (WMA, 2008), in the medical field, there has been a lot of progress. It has been proposed moral principles and practices adequate to every research area. There is common agreement in the scientific community in principles about proper scientific work, scientific integrity, and knowledge production practices that we will obey in this research.

In the following, we will examine some specific ethical issues related to the main subject of our research.

7.1 Ethics in Data Mining

Data Mining techniques allow considerable access to data. In (Fule et al., 2004) is stated that "The process of generating rules through a mining operation becomes an ethical issue when the results are used in decision making processes that effect people, or when mining customer data unwittingly compromises the privacy of those customers".

In data mining research, there are a substantial number of databases that could be considered ethically sensitive, for example in the case of medical research. The problem for data mining researchers is that investigations using knowledge discovery tools are commonly
open ended – it is not possible to know what will be found until it is discovered. Moreover, many useful investigations require the use of real data.

7.2 Ethics when working with documents and online information

There is a growing concern regarding the use of sensitive information stored electronic text documents. For example, Olson (Olson, 2008) took under consideration the ethical aspects of web mining blogs. They note that not only the privacy but, there are other issues, for example, price discrimination. "After identifying price sensitivity by group through data mining, the seller may offer special prices to specific customer groups" (Olson, 2008).

A main ethical concern is in the medical area, since the patient information must be keep confidential. Suominen et. al. (Suominen et al., 2006) discuss the ethical considerations when using text mining with nursing documentation. The principal concern is to keep confidentiality of patients while using text mining tools.
BIBLIOGRAPHY


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