

# Quantitative Analysis

Quantitative analysis using the electron microprobe involves measuring the intensities of X-ray lines generated from your unknown sample, and comparing these to the same lines in suitable standards, using identical instrumental conditions, such as:

- \* Accelerating voltage
- \* beam current
- \* specimen geometry
- \* beam size
- \* coating thickness

## **A number of factors are important components of quantitative analysis:**

- Selection of suitable standards
- Selection of suitable crystals and order of analysis
- Choice of appropriate analytical conditions
- Background selection/correction
- Matrix corrections (ZAF, Phi-Rho-Z)

# Quantitative WDS analysis

A simplified approximation of the principle of WDS analysis is as follows:

$$C_A(\text{sp}) = [I_A(\text{sp})/I_A(\text{st})]C_A(\text{st})$$

Where

$C_A(\text{sp})$  = concentration in specimen

$C_A(\text{st})$  = concentration in standard

$I_A(\text{sp})$  = X-ray intensity in specimen

$I_A(\text{st})$  = X-ray intensity in standard

$I_A(\text{sp})/ I_A(\text{st})$  is known as the K ratio

# Approach to WDS Analysis

## 1. Choose appropriate standards for analysis.

-Good characteristics for standards??

-Pure elements can be unsuitable. High matrix corrections, chemical bonding effects, difficult to polish, oxidation, may not exist in natural form.

-Synthetic compounds can be used. Has the advantage of assured purity. Homogeneity on a very fine scale is desirable.

-Some natural minerals can be well characterized, or compositions can be determined from theoretical formulas and can be used as standards. Must be homogeneous.

-Well-characterized complex phases can be used as reference materials to verify calibration. Kakanui phases.

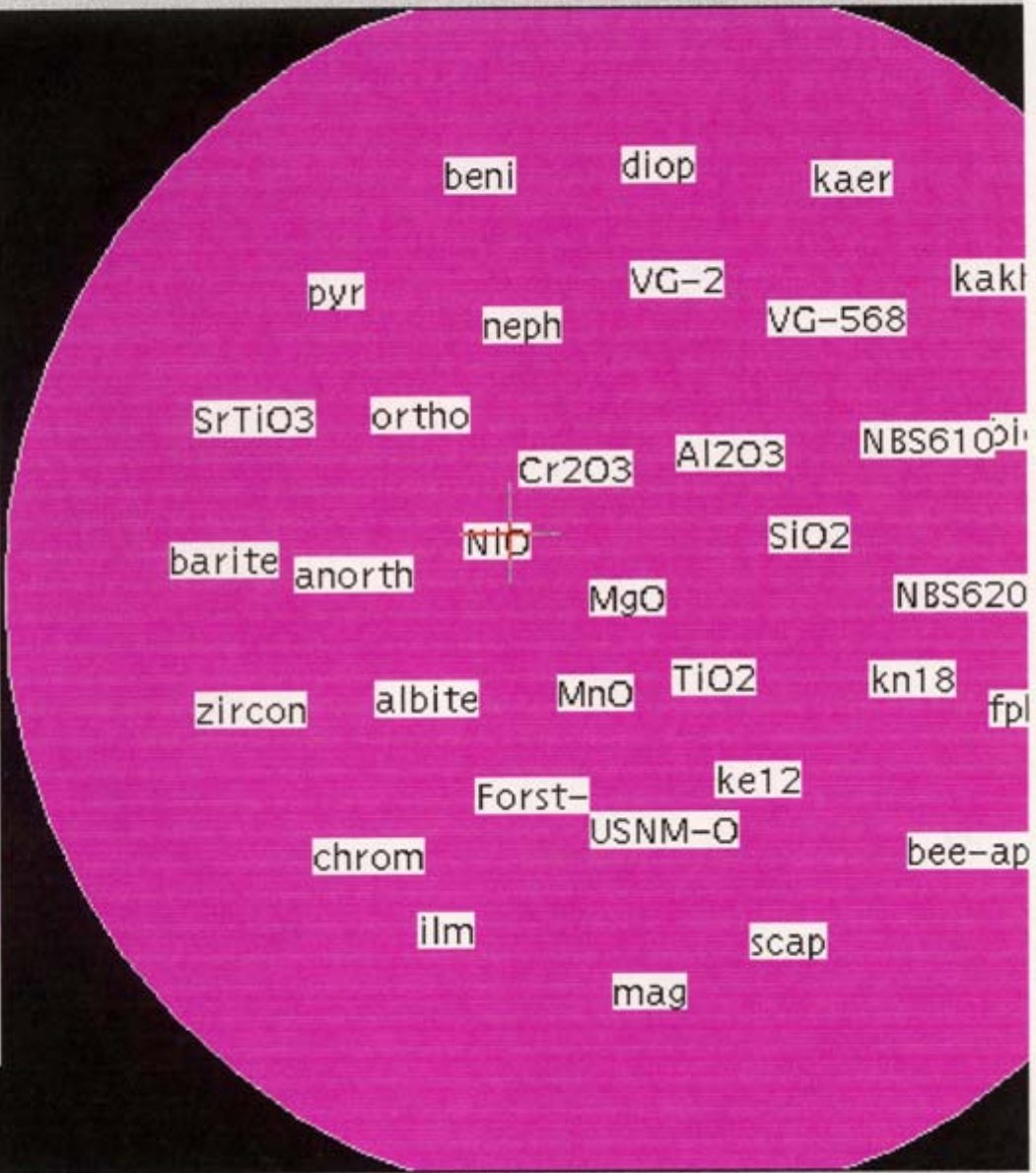
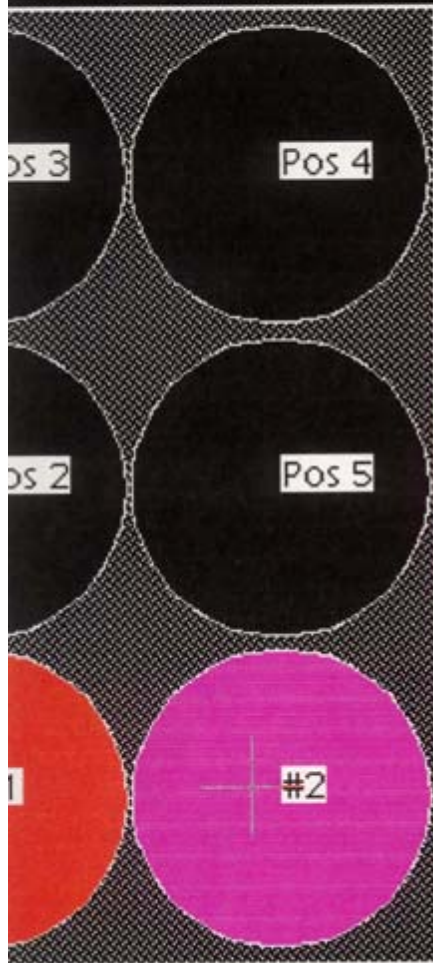


STAGE DISPLAY

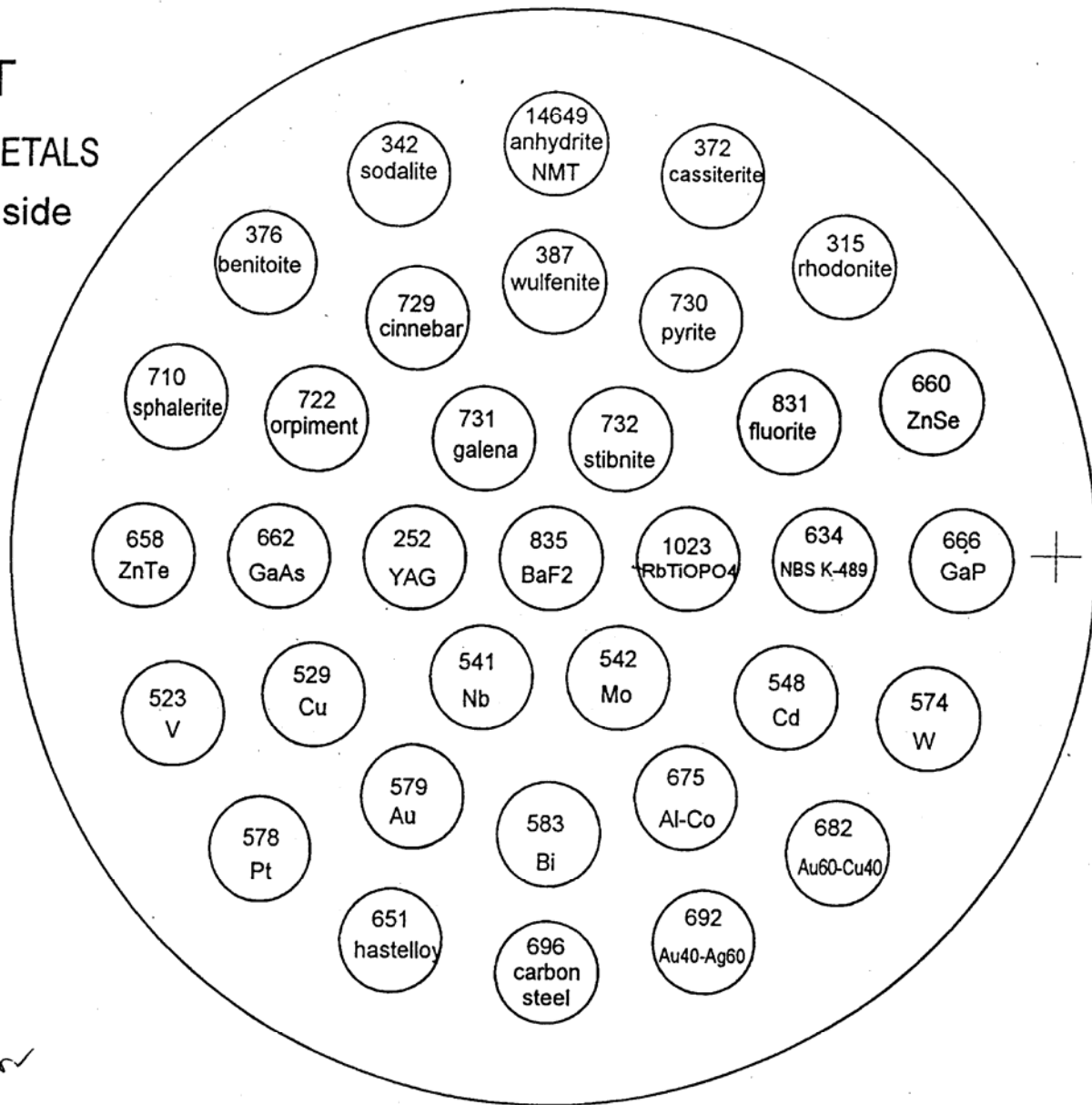
Holder: ▾ Six Position

Type: ▾ Standard

Reference



NMT  
ORES & METALS  
polished side



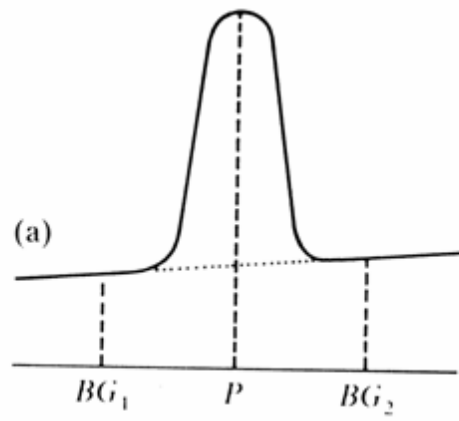
See back for  
compositions

## **2. Peak search and choose appropriate background values.**

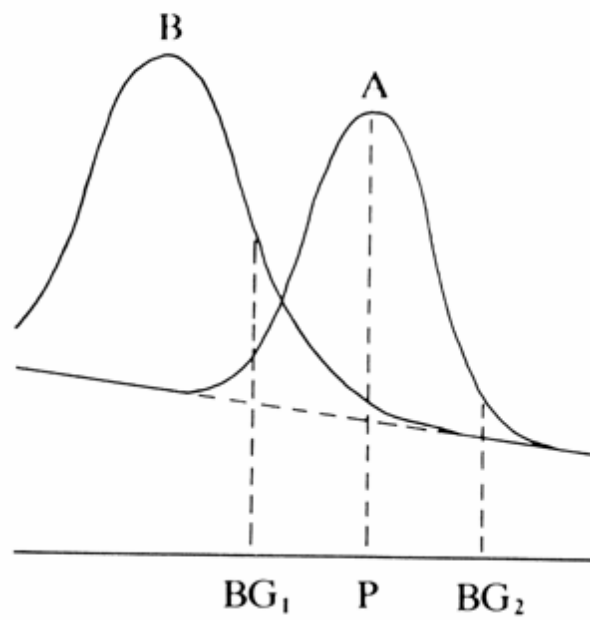
-Measured peak intensities include a contribution from the background. This must be evaluated. Preferable to measure backgrounds on both sides of the peak, but can use one side only to save spectrometer wear.

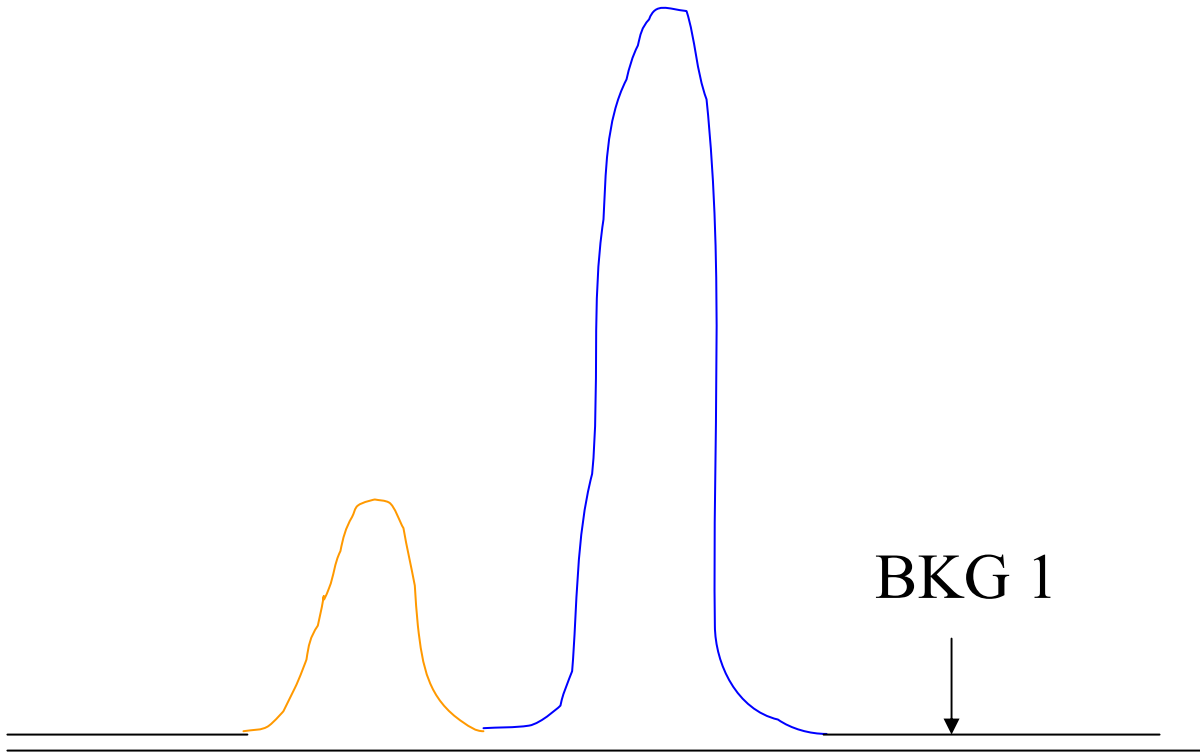
-Problems can arise if standards have different backgrounds than unknowns (ie. Fe interference on F).

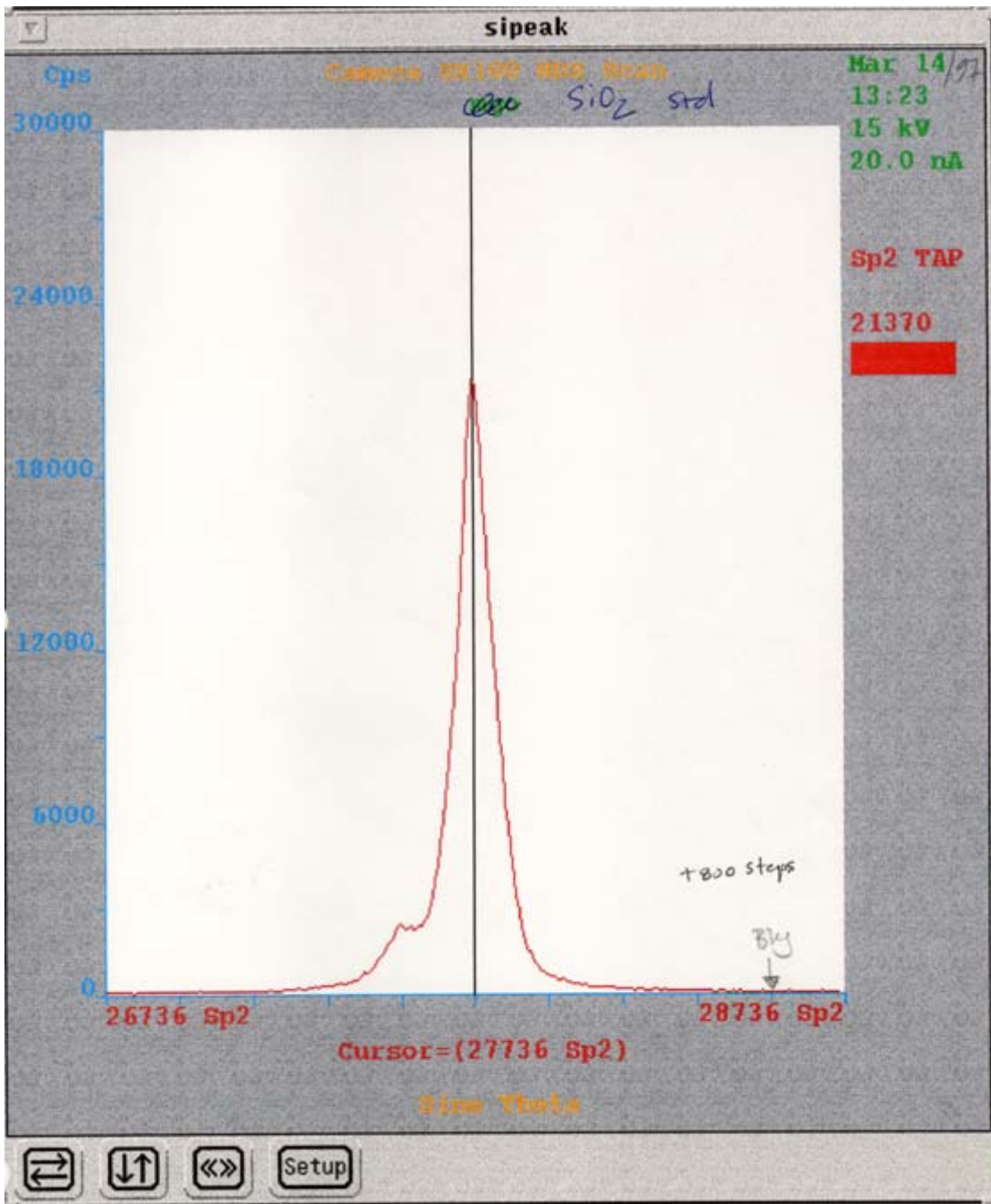




*Quantitative WD analysis*







mgpeak2

Cps

Camacho BK100 RGS Scan

Mar 14

mg

11:06

15 kV

4000

3200

2400

1600

800

36009 Sp2

Bkg #2

-2500

Cursor=(38498 Sp2)

41009 Sp2

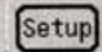
Bkg 1

+2500

Sp2 TAP

2826

2θ



### **3. Choose suitable crystals and order of analysis.**

A. Choose suitable crystals for each element

B. Minimize analysis time

C. Organize order of analysis in order to minimize spectrometer wear.

PERIODIC TABLE - SP2 - TAP

1 H	Order ▾ 1																Ka	Kb	Ray Filter					HV (kV) 15.0					2 He					
3 Li	4 Be																	La	Lb	Lc	Li	Ln						5 B	6 C	7 N	8 O	9 F	10 Ne	
11 Na	12 Mg																	Lb4	Lb3	Lb6	Lb2	Lb7						13 Al	14 Si	15 P	16 S	17 Cl	18 Ar	
19 K	20 Ca	21 Sc	22 Ti	23 V	24 Cr	25 Mn	26 Fe	27 Co	28 Ni	29 Cu	30 Zn	31 Ga	32 Ge	33 As	34 Se	35 Br	36 Kr																	
37 Rb	38 Sr	39 Y	40 Zr	41 Nb	42 Mo	43 Tc	44 Ru	45 Rh	46 Pd	47 Ag	48 Cd	49 In	50 Sn	51 Sb	52 Te	53 I	54 Xe																	
55 Cs	56 Ba	57 La	72 Hf	73 Ta	74 W	75 Re	76 Os	77 Ir	78 Pt	79 Au	80 Hg	81 Tl	82 Pb	83 Bi	84 Po	85 At	86 Rn																	
87 Fr	88 Ra	89 Ac																																
CAMECA			58 Ce	59 Pr	60 Nd	61 Pm	62 Sm	63 Eu	64 Gd	65 Tb	66 Dy	67 Ho	68 Er	69 Tm	70 Yb	71 Lu																		
			90 Th	91 Pa	92 U	93 Np	94 Pu	95 Am	96 Cm	97 Bk	98 Cf	99 Es	100 Fm	101 Md	102 No	103 Lr																		

PERIODIC TABLE - SP1 - PET

1 H	Order <input type="text" value="1"/>															2 He																															
3 Li	4 Be	<table border="1"> <tr> <td>Ka</td> <td>Kb</td> <td colspan="3">Ray Filter</td> </tr> <tr> <td>La</td> <td>Lb</td> <td>Lc</td> <td>Li</td> <td>Ln</td> </tr> <tr> <td>Lb4</td> <td>Lb3</td> <td>Lb6</td> <td>Lb2</td> <td>Lb7</td> </tr> <tr> <td>Lb10</td> <td>Lb9</td> <td>Lc2</td> <td>Lc3</td> <td>Lc4</td> </tr> <tr> <td>Ma</td> <td>Mb</td> <td>Mc</td> <td>Mz</td> <td></td> </tr> </table>										Ka	Kb	Ray Filter			La	Lb	Lc	Li	Ln	Lb4	Lb3	Lb6	Lb2	Lb7	Lb10	Lb9	Lc2	Lc3	Lc4	Ma	Mb	Mc	Mz		5 B	6 C	7 N	8 O	9 F	10 Ne	HV (kV) 15.0				
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PERIODIC TABLE - SP3 - LLIF

1 H	Order <input type="button" value="v"/> 1																2 He																									
3 Li	4 Be	<table border="1"> <tr> <td>Ka</td> <td>Kb</td> <td colspan="3">Ray Filter</td> </tr> <tr> <td>La</td> <td>Lb</td> <td>Lc</td> <td>Ll</td> <td>Ln</td> </tr> <tr> <td>Lb4</td> <td>Lb3</td> <td>Lb6</td> <td>Lb2</td> <td>Lb7</td> </tr> <tr> <td>Lb10</td> <td>Lb9</td> <td>Lc2</td> <td>Lc3</td> <td>Lc4</td> </tr> <tr> <td>Ma</td> <td>Mb</td> <td>Mc</td> <td>Mz</td> <td></td> </tr> </table>										Ka	Kb	Ray Filter			La	Lb	Lc	Ll	Ln	Lb4	Lb3	Lb6	Lb2	Lb7	Lb10	Lb9	Lc2	Lc3	Lc4	Ma	Mb	Mc	Mz		HV (kV) 15.0					10 Ne
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<input type="button" value="CAMECA"/>			58 Ce	59 Pr	60 Nd	61 Pm	62 Sm	63 Eu	64 Gd	65 Tb	66 Dy	67 Ho	68 Er	69 Tm	70 Yb	71 Lu																										



# **Matrix corrections: Bence-Albee Alpha Coefficients**

Used to be widely used for electron microprobe quantitative analysis. Has been replaced by other methods.

Empirical correction factors. Are only valid for a given accelerating voltage and X-ray take-off angle.

# Matrix Corrections

The matrix of the sample (ie. the chemical makeup of the sample) has a strong effect on the X-rays generated by any element. Must apply matrix corrections to uncorrected concentrations (K ratios) to obtain "true" compositions.

Three main controlling parameters:

Z - atomic number

A - absorption

F - fluorescence

# Z corrections

Related to the dependence of the efficiency with which X-rays are excited on the mean atomic number of the sample.

Two distinct phenomena:

1. Electron penetration
2. Backscattering

## **1. Electron penetration.**

Proportionately more electrons produce X-rays when interacting with a sample of higher atomic number. So, if  $Z$  of a sample is higher than  $Z$  of a standard, the uncorrected concentration of the unknown must be corrected downwards.

## **2. Backscattering.**

High- $Z$  material produced more BSE than low  $Z$  material. So, a higher  $Z$  material will have less X-rays produced than a low  $Z$  material. This offsets, and normally outweighs, the electron penetration effect.

Incident electrons lose energy by interacting with bound electrons within the sample

# of electrons per atom =  $Z$

Atomic mass per electron =  $A/Z$

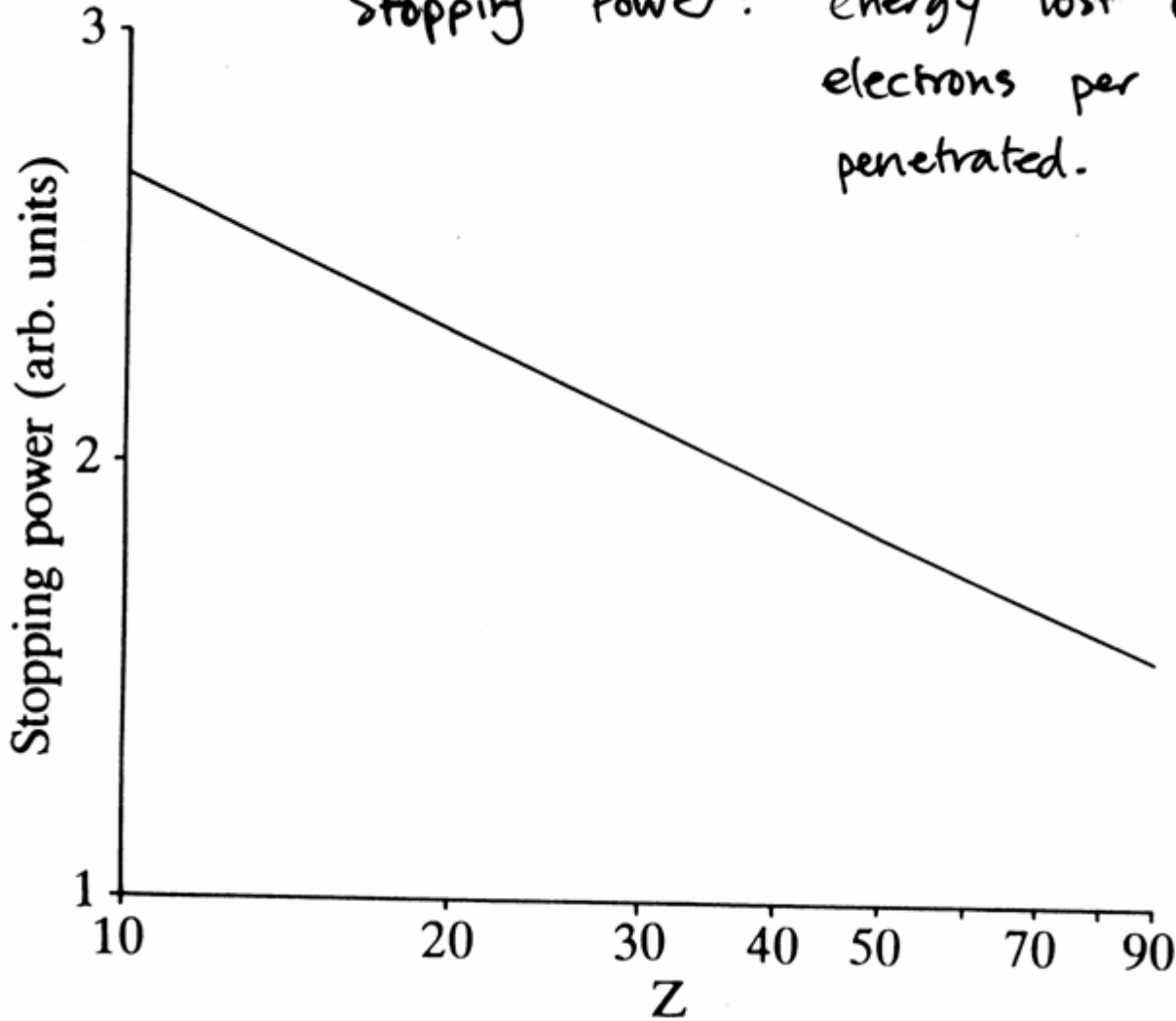
$A/Z$  increases with increasing  $Z$

So:

Mass penetrated by incident electrons **increases** with **increasing**  $Z$

----->>> X-rays intensities increase with increasing  $Z$

Energy lost by incident electrons  
per unit mass penetrated



## Absorption corrections

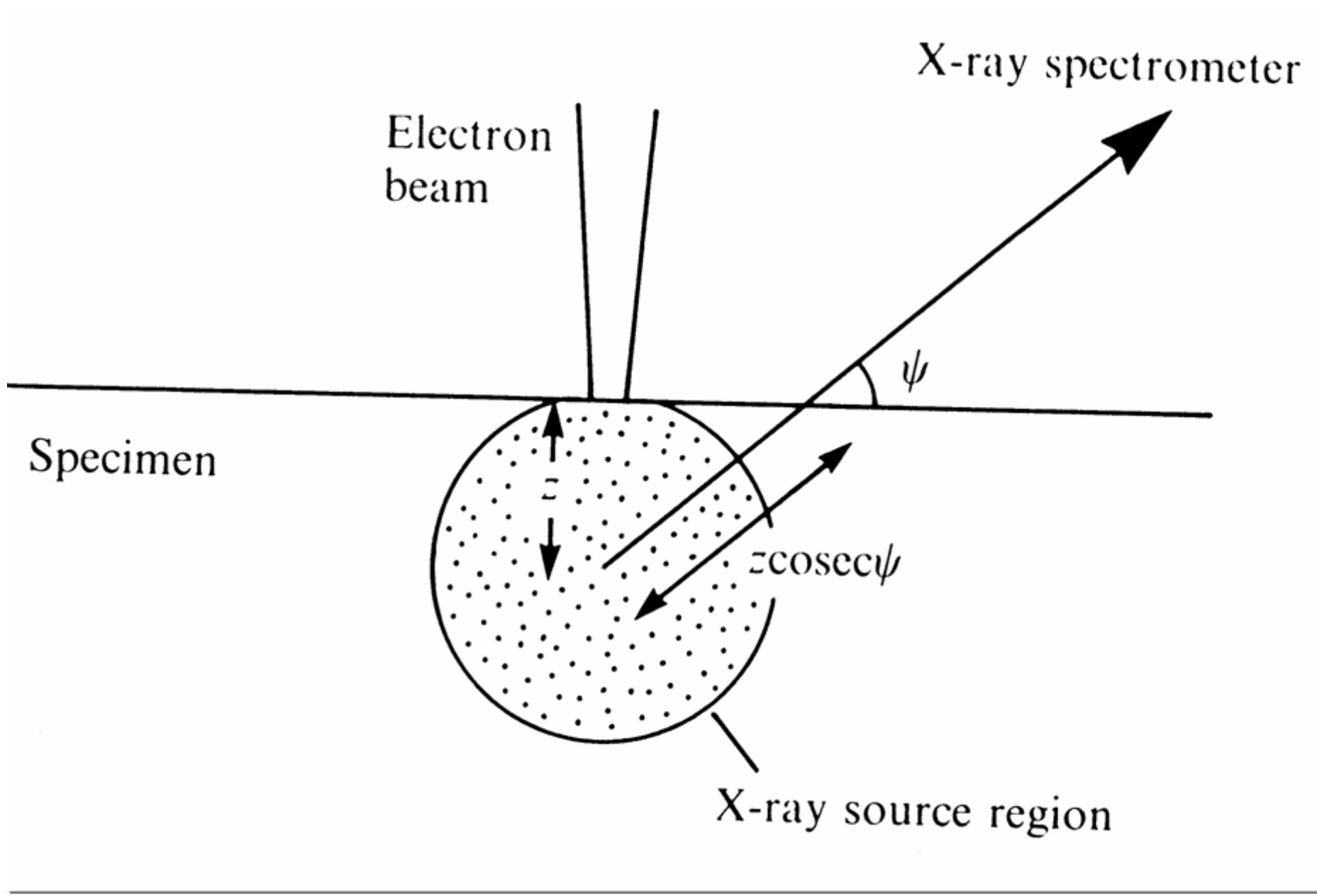
X-rays must travel through some amount of sample before exiting the sample surface. X-rays can be absorbed by the sample during this travel.

$$\chi = \mu \operatorname{cosec} \psi$$

$\chi$  = absorption parameter (khi)

$\mu$  = mass absorption coefficient (mu)

$\psi$  = takeoff angle (psi)



# X-rays produced at depth Z

$$\text{Intensity} = I_0 (-\chi^{\rho Z})$$

Absorption parameter  
 $\mu \operatorname{cosec} \psi$

$\rho$  = density (rho)

Z = depth

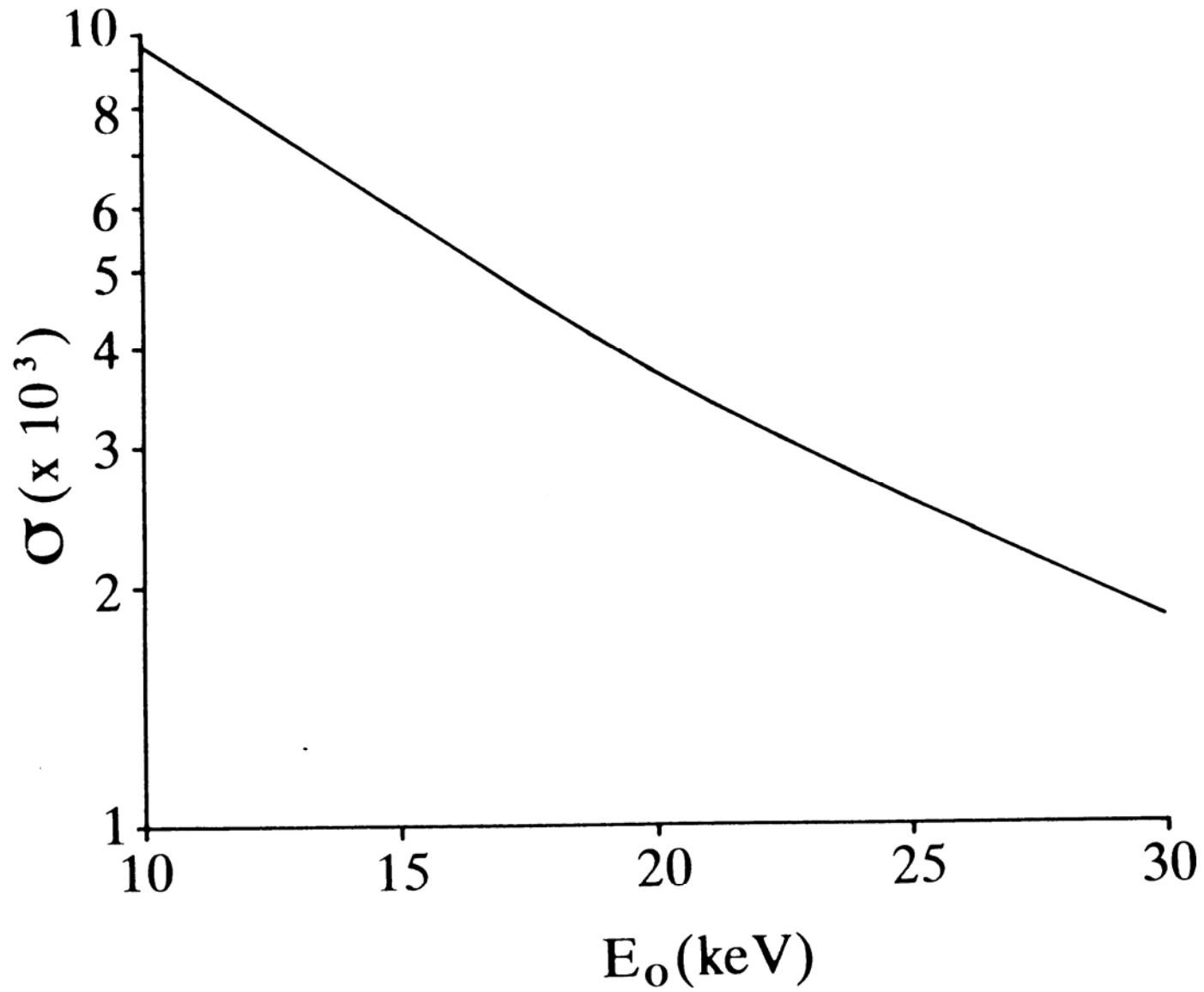
Depth-distribution production of X-rays must be known.

Approximated by:

$$\text{Intensity} = I_0 (-\sigma\rho Z)$$

Where  $\sigma$  is the absorption parameter

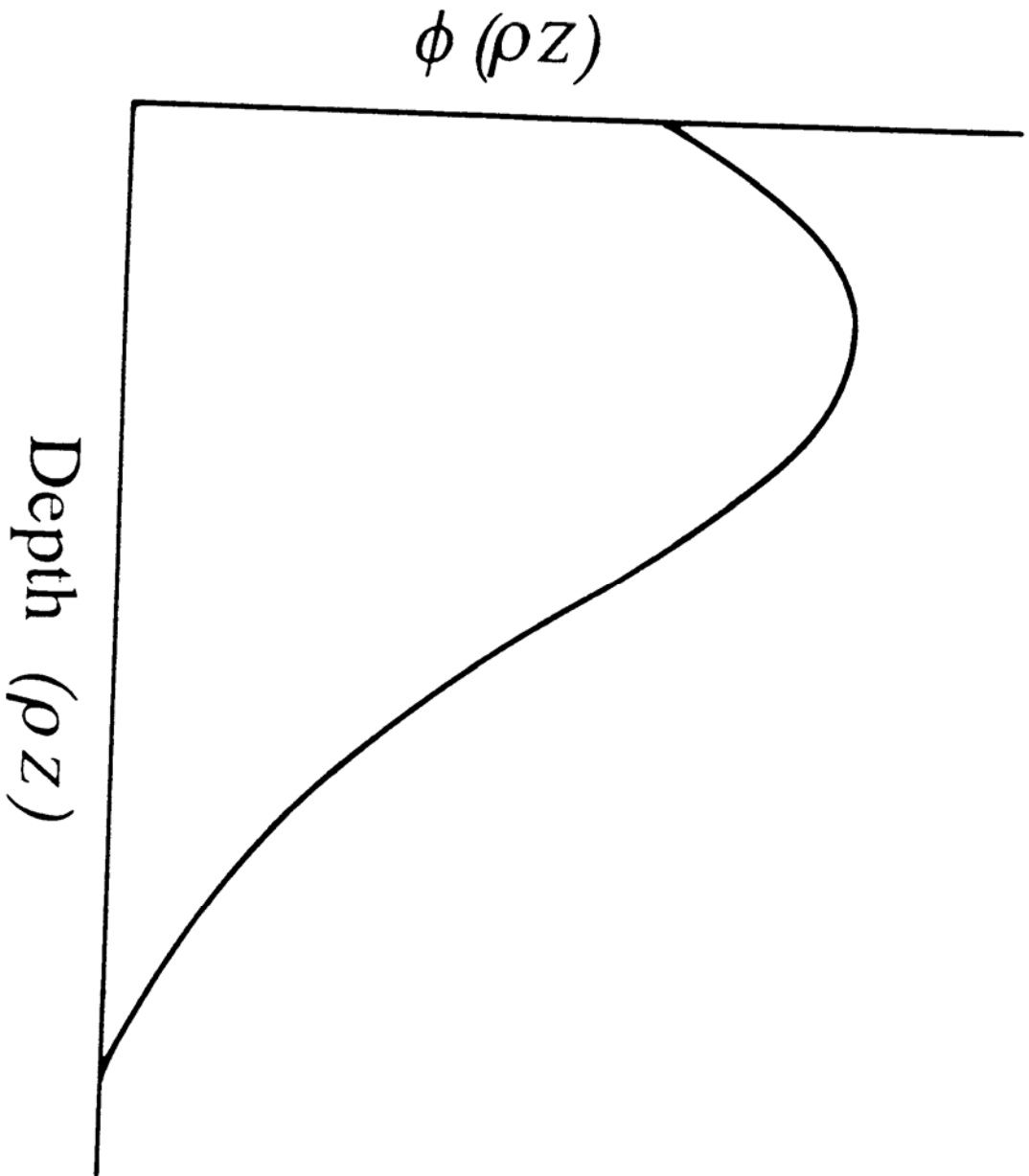




More sophisticated methods to calculate absorption are derived from expressions which better represent the depth distribution of X-ray production.

Termed Phi-Rho-Z  $\phi(\rho Z)$

Depth-distribution function that is defined as the X-ray intensity generated by a thin layer at depth  $z$  relative to an isolated layer of the same thickness.

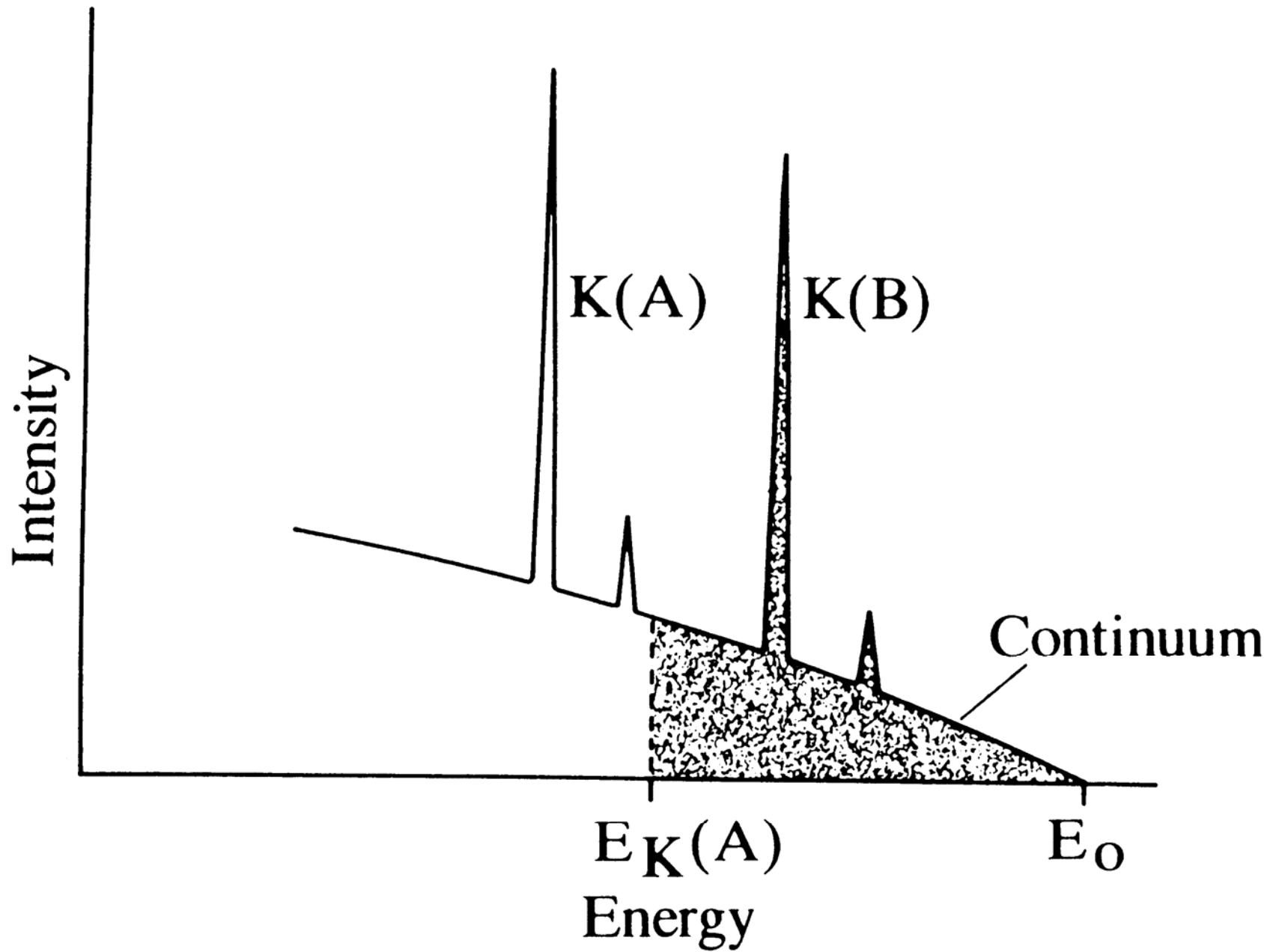


## Fluorescence corrections

Characteristic X-rays of a given element can be excited by other X-rays when the energy of the latter exceeds the critical excitation energy of the former. Can be caused either by continuous or by characteristic X-rays.

For example, Ni K $\alpha$  X-rays (7.48 keV) can excite Fe (critical excitation energy 7.11 keV). But, Fe K $\alpha$  X-rays (6.4 keV) cannot excite Ni (critical excitation energy 8.33 keV).

Correction factors can be calculated. In geological samples, this correction is relatively small. The effect decreases with decreasing atomic number. More important in metallurgical samples.



Correction calculations are iterative. A composition must first be assumed. Then, correction factors are calculated from that assumed composition, and a new composition is determined. Typically, three to six iterations are made. This requires **COMPUTERS!**

# Unanalyzed Components

Our electron probe cannot analyze H, He, Li, Be, B, C, N, and O.

This is an issue when the unknown sample contains one or more of these elements. For example, silicate rock samples all contain a large amount of O. Some also contain H<sub>2</sub>O. Carbonate rock samples contain C and O.

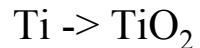
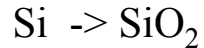
Unanalyzed components can be treated in 2 ways:

## **-Difference.**

Assuming that the difference between the electron microprobe total and 100% is due to the unanalyzed component (s).

## **-Stoichiometry.**

Appropriate amount of the unanalyzed component is allocated to the analyzed elements in the sample. For instance, O in a silicate rock.



etc...

Some minerals, such as clays, contain H<sub>2</sub>O in addition to H, and the recalculation is more difficult.

CAMECA software handles a large number of geological recalculations.

# Choice of conditions for Quantitative Analysis

## -Electron acceleration

Must be higher than the excitation potential of elements to be analyzed. Preferably twice this value.

Advantages of higher kV

Better analytical statistics and precision

Better peak/background, leading to better detection limits

Disadvantages of higher kV

Decreased spatial resolution

Increased absorption corrections

**For geological samples, typically use 15 kV.** Can use lower kV for light element analysis

## -Beam current

High beam current yields higher X-ray intensities. But... can lead to sample damage.

**For geological samples, typically use 20 nA.** For glasses, use 10 or 15 nA.



# Special Cases

## **A. Tilted samples**

If necessary, corrections can be made for analysis to tilted samples. Tilt angle must be precisely known.

## **B. Broad-beam analysis**

Can broaden beam to determine average compositions. However, area must be <100 microns in order to not run into spectrometer defocalization. However, ZAF corrections are not accurate for a combination of phases. However, this technique can be useful for rapid, semiquantitative analysis.

## **C. Whole rock analysis**

Fuse samples into a glass. Should not compete with conventional bulk rock analysis techniques, but can sometimes be useful.

## **D. Particle analysis**

Small particles mounted on carbon backing can be analysed. Net X-ray intensities can be reduced relative to a flat standard, but calibrations may be done using X-ray ratios. Also, modified ZAF corrections can be made to reflect particle geometry.

## **E. Thin sample analysis**

Spatial resolution can be increase by preparation of a very thin (100 nm) sample wafer. If sample is sufficiently thin, ZAF corrections can be neglected.

## **F. Fluid inclusions**

Frozen fluid inclusions can be analyzed using a cryo-stage. Must prepare frozen standards. Must use very low beam currents (1 nA).

## **G. Valence determinations**

Peak shifts can be observed for some elements related to valence of the element.

Fe<sup>+2</sup>/Fe<sup>+3</sup> using L peaks

S<sup>-2</sup>/S<sup>6+</sup> ratio in glasses by 0.003 angstrom shift in S K alpha peak.

